

**Question Bank of Numerical Analysis for the Third Communication Stage in  
the Physics Dep. of the Second Semester:**

1. Use the Newton-Raphson method to find an approximation of the root of the function  $f(x) = \cos(x) - x^2$ , starting from the initial guess  $x_0 = 1$ . Perform three iterations and show the intermediate approximations.
2. Use the secant method to find a root of the equation  $f(x) = e^x - x^3 - 5$  within the interval  $[1, 2]$ . Perform four iterations and show the intermediate approximations.
3. Given the system of linear equations:

$$4x - y + 3z = 8$$

$$x + 2y - 3z = -1$$

$$2x - y + z = 3$$

Use the Gauss-Jordan elimination method to solve this system. Show each step of the elimination process and the final solution.

4. Use the fixed-point iteration method to find a root of the equation  $x = e^{(-x)}$  within the interval  $[0, 1]$ . Perform four iterations and show the intermediate approximations.
5. Consider the function  $f(x) = x^3 - 2x^2 + x - 1$ . Use the bisection method to find a root of this function within the interval  $[1, 2]$ . Perform three iterations and show the intermediate steps and approximations.
6. Given the system of linear equations:

$$3x + 2y - z = 1$$

$$2x - 2y + 4z = -2$$

$$-x + 0.5y - z = 0$$

Use the Gauss elimination method to solve this system. Show each step of the elimination process and the final solution.

7. Use the Newton-Raphson method to find an approximation of the root of the function  $f(x) = x^3 - 3x + 1$ , starting from the initial guess  $x_0 = 1$ . Perform two iterations and show the intermediate approximations.

8. Use the bisection method to find a root of the function  $f(x) = x^3 - 4x^2 + 5x - 2$  within the interval  $[0, 2]$ . Perform four iterations and show the intermediate steps and approximations.

9. Given the system of linear equations:

$$2x + 3y - z = 4$$

$$x - 2y + 3z = 7$$

$$3x + 2y + 4z = 10$$

Use the Gauss-Seidel method to solve this system. Show each step of the iterative process and the final solution after three iterations.

10. Use the Newton-Raphson method to find an approximation of the root of the function  $f(x) = x^3 - 2x - 5$ , starting from the initial guess  $x_0 = 2$ . Perform three iterations and show the intermediate approximations.

11. Use the Newton-Raphson method to find an approximation of the root of the equation  $f(x) = x^3 - 4x - 9$ , starting from the initial guess  $x_0 = 2$ . Perform five iterations and show the intermediate approximations.

12. Use the fixed-point iteration method to find a root of the equation  $x = \cos(x)$  within the interval  $[0, \pi/2]$ . Perform four iterations and show the intermediate approximations.

13. Use the bisection method to find a root of the function  $f(x) = x^3 - 6x^2 + 11x - 6$  within the interval  $[1, 2]$ . Perform five iterations and show the intermediate steps and approximations.

14. Given the system of linear equations:

$$3x + 2y - z = 1$$

$$2x - 4y + 3z = -5$$

$$-x + y - z = 0$$

Use the Jacobi method to solve this system. Show each step of the iterative process and the final solution after three iterations.

15. Use the secant method to find a root of the equation  $f(x) = x^3 - 5x + 2$  within the interval  $[0, 1]$ . Perform five iterations and show the intermediate approximations.

**16.** Given the system of linear equations:

$$2x - 3y + z = 7$$

$$x + 2y + 2z = 10$$

$$-x - y + 3z = 5$$

Use the LU decomposition method to solve this system. Show each step of the decomposition process and the final solution.

**17.** Use the fixed-point iteration method to find a root of the equation  $x = 2 - e^{(-x)}$  within the interval  $[0, 2]$ . Perform five iterations and show the intermediate approximations.

**18.** Use the Newton-Raphson method to find an approximation of the root of the equation  $f(x) = 2x^3 - 5x - 3$ , starting from the initial guess  $x_0 = 1.5$ . Perform four iterations and show the intermediate approximations.

**19.** Use the fixed-point iteration method to find a root of the equation  $x = \ln(x)$  within the interval  $[1, 2]$ . Perform four iterations and show the intermediate approximations.

**20.** Use the bisection method to find a root of the function  $f(x) = x^4 - 3x^2 + 2x - 1$  within the interval  $[0, 1]$ . Perform five iterations and show the intermediate steps and approximations.

**21.** Given the system of linear equations:

$$4x - 2y + 3z = 10$$

$$-x + 3y - 2z = -5$$

$$2x - y + 4z = 3$$

Use the Gauss-Seidel method to solve this system. Show each step of the iterative process and the final solution after four iterations.

**22.** Use the secant method to find a root of the equation  $f(x) = \sin(x) - x$  within the interval  $[1, 2]$ . Perform five iterations and show the intermediate approximations.

**23.** Given the system of linear equations:

$$3x - y + 2z = 8$$

$$x + 2y - 4z = -7$$

$$-2x + y - 3z = 1$$

Use the Gauss-Jordan elimination method to solve this system. Show each step of the elimination process and the final solution.

24. Use the fixed-point iteration method to find a root of the equation  $x = 2 + 3\sin(x)$  within the interval  $[0, 1]$ . Perform five iterations
25. Use the fixed-point iteration method to find a root of the equation  $x = 2 + 3\sin(x)$  within the interval  $[0, 1]$ . Perform five iterations and show the intermediate approximations.
26. Use the Newton-Raphson method to find an approximation of the root of the equation  $f(x) = 3x^3 - 5x^2 + 2$ , starting from the initial guess  $x_0 = 0.5$ . Perform four iterations and show the intermediate approximations.
27. Use the fixed-point iteration method to find a root of the equation  $x = \ln(2 + x)$  within the interval  $[1, 2]$ . Perform five iterations and show the intermediate approximations.
28. Approximate the definite integral  $\int_0^\pi \sin(x) dx$  using the composite midpoint rule with eight subintervals. Show the step-by-step process and the final approximation.
29. Approximate the derivative of the function  $f(x) = \sin(2x)$  at  $x = \pi/6$  using the three-point central difference formula. Show the step-by-step calculations and the final approximation.
30. Approximate the definite integral  $\int_0^3 x^2 dx$  using the composite Simpson's rule with eight subintervals. Show the step-by-step process and the final approximation.
31. Solve the initial value problem  $dy/dx = x^2 + y$ ,  $y(0) = 1$ , using the fourth-order Adams-Bashforth method with a step size of 0.2. Calculate the approximate value of  $y$  at  $x = 1$ , showing the intermediate steps.
32. Approximate the derivative of the function  $f(x) = \sqrt{x}$  at  $x = 4$  using the five-point stencil method. Show the step-by-step calculations and the final approximation.
33. Approximate the definite integral  $\int_0^6 e^{-x^2} dx$  using the composite trapezoidal rule with four subintervals. Show the step-by-step process and the final approximation.

34. Solve the initial value problem  $dy/dx = x^2 + y, y(0) = 1$ , using the fourth-order Runge-Kutta method. Calculate the approximate value of  $y$  at  $x = 0.1$ , showing the intermediate steps.
35. Approximate the definite integral  $\int_0^1 \sin(x) dx$  using the composite midpoint rule with six subintervals. Show the step-by-step process and the final approximation.
36. Solve the initial value problem  $dy/dx = x^2 + y, y(0) = 1$ , using the fourth-order Runge-Kutta method. Calculate the approximate value of  $y$  at  $x = 0.5$ , showing the intermediate steps.
37. Approximate the derivative of the function  $f(x) = \sin(x)$  at  $x = \pi/4$  using the three-point forward difference formula. Show the step-by-step calculations and the final approximation.
38. Approximate the definite integral  $\int_0^2 x^2 dx$  using the composite Simpson's rule with four subintervals. Show the step-by-step process and the final approximation.
39. Solve the initial value problem  $dy/dx = x^2 + y, y(0) = 1$ , using the Euler's method with a step size of 0.1. Calculate the approximate value of  $y$  at  $x = 0.4$ , showing the intermediate steps.
40. Approximate the definite integral  $\int_1^3 e^x dx$  using the composite trapezoidal rule with six subintervals. Show the step-by-step process and the final approximation.
41. Approximate the derivative of the function  $f(x) = e^{(-2x)}$  at  $x = 1$  using the three-point backward difference formula. Show the step-by-step calculations and the final approximation.
42. Approximate the definite integral  $\int_0^1 \ln(x) dx$  using the composite trapezoidal rule with eight subintervals. Show the step-by-step process and the final approximation.
43. Solve the initial value problem  $dy/dx = x^2 + y, y(0) = 1$ , using the second-order Runge-Kutta method with a step size of 0.1. Calculate the approximate value of  $y$  at  $x = 0.5$ , showing the intermediate steps.
44. Approximate the definite integral  $\int_0^2 e^{(-x)} dx$  using the composite trapezoidal rule with ten subintervals. Show the step-by-step process and the final approximation.

45. Solve the initial value problem  $dy/dx = x^2 + y$ ,  $y(0) = 1$ , using the fourth-order Runge-Kutta method with a step size of 0.2. Calculate the approximate value of  $y$  at  $x = 0.8$ , showing the intermediate steps.
46. Approximate the definite integral  $\int_0^{\pi/2} \cos(x) dx$  using the composite midpoint rule with ten subintervals. Show the step-by-step process and the final approximation.
47. Solve the initial value problem  $dy/dx = x^2 + y$ ,  $y(0) = 1$ , using the second-order Runge-Kutta method with a step size of 0.2. Calculate the approximate value of  $y$  at  $x = 0.6$ , showing the intermediate steps.
48. Approximate the definite integral  $\int_0^4 x^3 dx$  using the composite Simpson's rule with twelve subintervals. Show the step-by-step process and the final approximation.
49. Approximate the derivative of the function  $f(x) = \cos(2x)$  at  $x = \pi/3$  using the three-point central difference formula. Show the step-by-step calculations and the final approximation.
50. Approximate the definite integral  $\int_0^5 e^{(-2x)} dx$  using the composite trapezoidal rule with fourteen subintervals. Show the step-by-step process and the final approximation.
51. Approximate the derivative of the function  $f(x) = e^{(-3x)}$  at  $x = 0$  using the three-point forward difference formula. Show the step-by-step calculations and the final approximation.