

Q1// Let W be a random variable having p.d.f. $W \sim N(0,1)$ and V random variable with p.d.f. $V \sim \chi_r^2$ and W and V are independent random variable, then the p.d.f. of $T = W/\sqrt{V/r}$ is known as T distribution proof that :

$$f(t) = \frac{\Gamma\left(\frac{r+1}{2}\right)}{\Gamma\left(\frac{r}{2}\right)\sqrt{r\pi}} \left(1 + \frac{t^2}{r}\right)^{-\frac{(r+1)}{2}} ; -\infty < T < \infty$$

Q2// In a r.s.s.n. show that $T = \bar{X}$ is efficient est. for

$$\phi(\theta) = \theta \text{ from } \exp(\theta)$$

Q3// Researchers are interested in the mean age of a certain population. A random sample of 10 individuals drawn from the population of interest has a mean of 27. Assuming that the population is approximately normally distributed with variance 20, can we conclude that the mean is different from 30 years, ($\alpha=0.05$) ?

where $Z_{0.025} = 1.96$, $Z_{0.10} = 1.28$, $Z_{0.05} = 1.64$

Q4 // Let x be a r.v. with p.d.f.

$$f(x) = \begin{cases} \left(\frac{2}{c}\right)^{-x} & x = 1, 2, 3, \dots \\ = 0 & o.w. \end{cases}$$

Find: $c=?$

Q5 // Find Bayes estimator for parameters of $N(\theta, \sigma^2)$ using non information prior probability. (-15 -Marks)

Q6// Let $x \sim U(-2,2)$ find the p.d.f. of $Y = |x|$?

Q7// Let x_1, x_2 , be a r.s.s. taken from $\exp(\theta)$ and $y_1 = x_1 + x_2$ and $y_2 = x_2$ and x_1 and x_2 are independent show that :-

1) $E[E(y_2/y_1)] = Ey_2$ 2) $V[E(y_2/y_1)] < V(y_2)$
 (15-Marks)

Q8// the results for the pre-and post-tests are below :

subject	1	2	3	4	5	6	7	8	9
Pre-test	78	67	56	78	96	82	84	90	87
Post-test	80	69	70	79	96	84	88	92	92

Is there difference between the mean of the pre – test and post-test , Use $\alpha=0.05$ (8-mark)

Q9// The mean of random experiment is 8.33 and $s^2 = 20.31$
 $\sum x^2=787$ find confidence interval %99 for mean.
 (7-mark)

Q10// If $f(x; \theta; \alpha) = \theta \alpha^\theta x^{-\theta-1}$ for $x \geq \alpha$ and $\theta \geq 1$ where θ and α are positive parameters of the distribution ,assume that α is known and that $x_1, x_2, x_3, \dots, x_n$ is a r.s. of size n from this distribution find moment and m.l.e. estimate for θ ,are they differ?
 (15-mark)

Q11// Find Bayes estimator for parameter of $N(\theta, \sigma^2)$, using information prior probability when σ^2

If $x \sim p_0(\theta)$, show that if we can apply (RAO-BLAK WELL THEORM) to $EE(x_1 / \sum_{i=1}^n x_i)$?

Q12// construct a 95% C.I. for the mean life of light bulbs given that a r.s. of size n=7 ,and with a s.d. =20 hours the average live time = 420 ,

$$Z_{0.025} = 1.96, t_{(0.025,6)} = 2.447, t_{(0.025,7)} = 2.365, \\ t_{(0.05,7)} = 1.895, Z_{0.05} = 1.645$$

Q13// Find Bayes estimator for parameter of $N(\theta, \sigma^2)$, using non information prior probability.

Q15// Let $y_1 < y_2 < y_3 < y_4$ be a order statistics of a r.v.s.4 taken from p.d.f. $f(x) = 1, 0 < x < 1$ and let $z_1 = y_2 - y_1, z_2 = y_2$

Find : 1) $g(y_1)$ 2) $E(y_1)$ 3) $h(z_1)$

Q16// let $y_1 < y_2 < y_3 < y_4 < y_5$ be the order statistics from $\exp\left(\frac{1}{\theta}\right)$, find 1) $g(y_2)$, 2) $g(y_{n-1})$

Q17// let $y_1 < y_2 < y_3 < y_4 < y_5$ be the order statistics from $\beta(2,1)$ find

1- largest value and expected

2- find smallest value

3- find pdf of median

4- the J.p.d.f. of $g(y_2/y_5)$

Q18// Let $y_1 < y_2 < y_3 < y_4$ be a order statistics of a r.v.s.4 taken from p.d.f. $f(x) = 1, 0 < x < 1$ and let $z_1 = y_2 - y_1, z_2 = y_2$

Find : 1) $g(y_1)$ 2) $E(y_1)$ 3) $h(z_1)$

Q19// let $(y_1 \leq y_2 \leq \dots \leq y_5)$ be the order statistics, of a random sample size 5 with p.d.f.

$$f(x, \theta) = e^{-(x-\theta)}, \theta < x < \infty$$

Find: $g(y_1), g(y_2), g(y_n)$ and $g(y_3, y_n)$

Q20// Let X_1 and X_2 have independent gamma distribution with parameters α, θ and β, θ respectively. If $z_1 = \frac{x_1}{x_1+x_2}$ and $Z_2 = X_1 + X_2$, find the j.p.d.f. of Z_1 , and Z_2 .

Q21// If the p.d.f. of X is $f(x) = \begin{cases} 2e^{-2x} & x > 0 \\ 0 & o.w \end{cases}$

Find the p.d.f. of $Y = \sqrt{X}$

Q22// If $X \sim N(\mu, \sigma)$ find the p.d.f. of $\frac{X-\mu}{\sigma}$

Q23// if $X_1 \sim b(n_1, p), X_2 \sim b(n_2, p)$ and independent. Let $Y_1 = X_1 + X_2$ and $Y_2 = X_2$ find the j.p.d.f of Y_1 and Y_2 ?

Q24// Among 157 African-American men, the mean systolic blood pressure was 146 mm Hg with a standard deviation of 27. We wish to know if on the basis of these data, we may conclude that the mean systolic blood pressure for a population of African-American is greater than 140. Use $\alpha=0.01$.

Q25// Researchers are interested in the mean age of a certain population. A random sample of 10 individuals drawn from the population of interest has a mean of 27. Assuming that the population is approximately normally distributed with variance 20, can we conclude that the mean is different from 30 years? ($\alpha=0.05$).

Q26// is \bar{x} unbiased estimation for $\theta(\theta) = \theta$ of

1- $Ber(\theta)$ 2- poisson (θ)

Q27// let $y_1 < y_2 < y_3$ be the order statistics of a r.s.s.3 from uniform(0, θ) are

1) $4y_1$ 2) $2y_2$ 3) $\frac{4}{3}y_3$ unbiased est. for θ

Q28// from $N(\theta, \sigma^2)$ find biased part for θ^2 if $T = \bar{x}^2$

Q29// from $un(0, \theta)$, find biased part for θ if $T = \bar{X}$

Q30// from $\exp(\theta)$ is \bar{x} unbiased est. in limit for θ