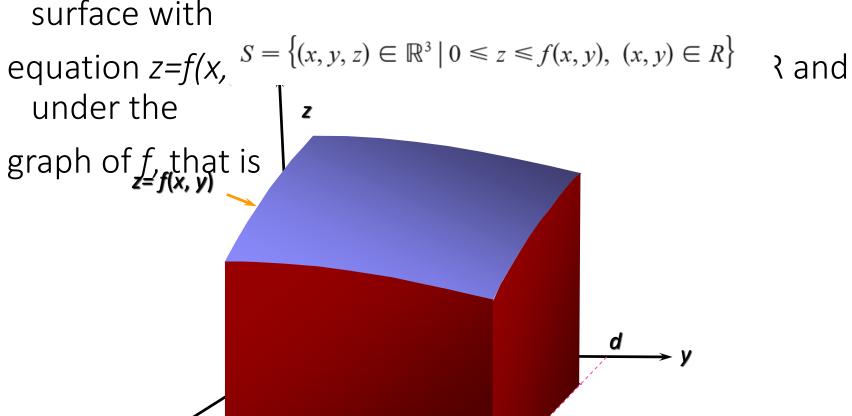
## Double Integral

Suppose that f(x,y) defined on a closed rectangle

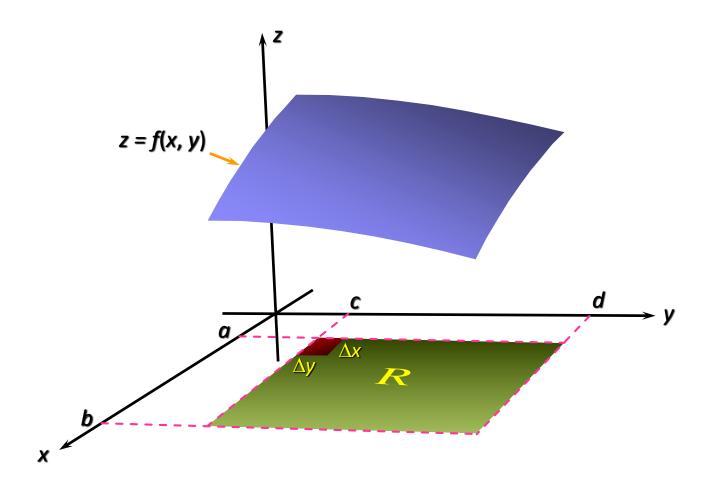
$$R = [a, b] \times [c, d] = \{(x, y) \in \mathbb{R}^2 \mid a \le x \le b, \ c \le y \le d\}$$

and we first suppose  $\mathsf{t}^{f(x,y) \geq 0}$  . The graph of f is a surface with

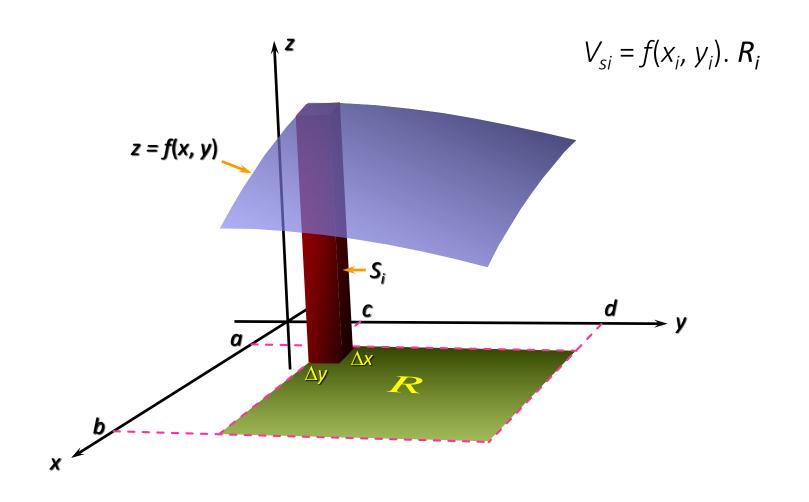


 Our goal is to find the volume of S. To find the volume of the solid under the surface, we can perform a Riemann sum of the volume S<sub>i</sub> of parallelepipeds with base

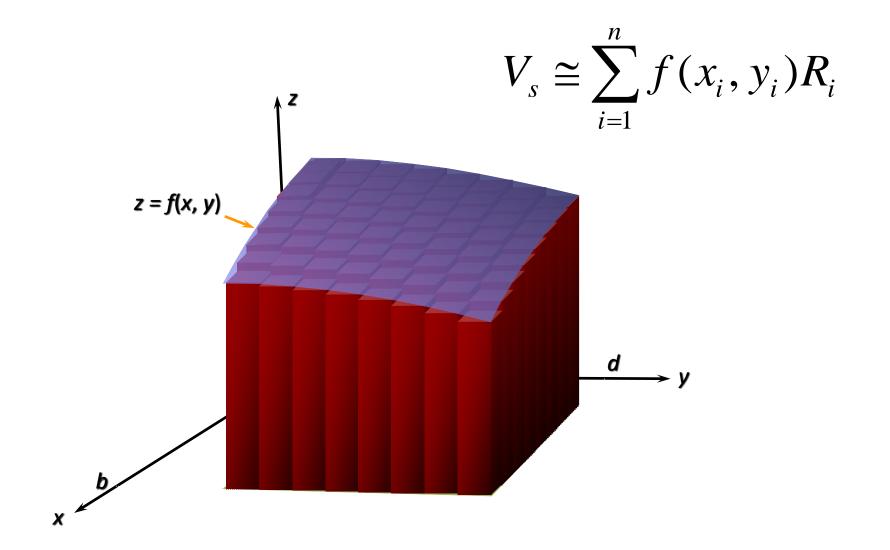
 $R_i = \Delta x \times \Delta y$  and height  $f(x_i, y_i)$ :



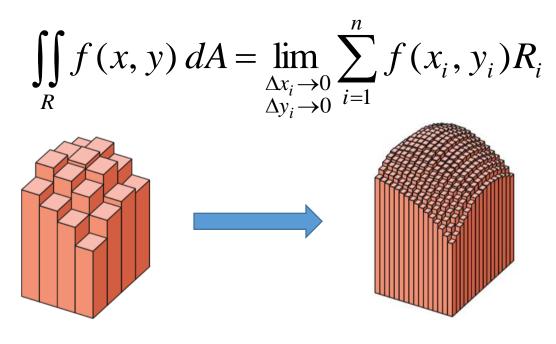
## A Geometric Interpretation of the Double Integral



## A Geometric Interpretation of the Double Integral



The limit of the Riemann sum obtained when  $\Delta x$  and  $\Delta y$  go to zero is the value of the double integral of f(x, y) over the region R and is denoted by



The double integral represent the volume above the region R and the upder the surface f(x,y).