

## Department of Mathematics

## College of Basic education

University of Salahaddin University -Erbil
Subject: Vector Analysis
Course Book: Second Year
Lecturer's name: Aween S. Karim
Academic Year: 2023-2024

## Course Book

| 1. Course name | Vector Analysis |
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| 2. Lecturer in charge | Awen S.abdollah Karim |
| 3. Department/ College | Mathematics/ Basic Education |
| 4. Contact | e-mail:awen.karim@su.edu.krd |
| 5. Time (in hours) per week | Theory: 4 |
| 6. Office hours |  |
| 7. Course code | B.Sc degree in mathematics from the University of Urmia in <br> 2008 <br> M.Sc degree in Numerical Analysis at the University of <br> Urmia in 2012 |
| 8. Teacher's academic <br> profile | Vector Analysis (vector space, Cross \& dot product, Limits <br> and Continuity of function with two variables, Partial <br> Derivative, Gradient Vectors...) |
| 9. Keywords |  |
| 10. Course overview: <br> Calculus weaves together previous study of algebra, geometry, and functions. The course <br> focuses on the mastery of critical skills and exposure to new skills necessary for success in <br> subsequent math courses. Calculus is a foundational course; it plays an important role in <br> the understanding of science, engineering, economics, and computer science, among <br> other disciplines. Calculus also provides important tools in understanding functions and <br> has led to the development of new areas of mathematics including real and complex <br> analysis, topology, and non-euclidean geometry. <br> This introductory calculus course covers differentiation and integration of functions of two <br> variable, with applications. |  |
| After completing this course, students should have developed a clear understanding of the <br> fundamental concepts of single variable calculus and a range of skills allowing them to <br> work effectively with the concepts. <br> The general objective of this course is to deeper understanding and working knowledge of <br> mathematics. also we have other aims such as awareness of applications of calculus in <br> mathematics and physics and to develop understanding of mathematics. moreover one of <br> the goals of the course is learn to think creatively, be able to attack a problem you have <br> not seen before, develop tools for that, develop a mathematical model for a given 'real <br> life' situation. |  |
| 11. Course objective: <br> 1. Analyze vectors in space <br> 2. Introduce basic ideas of parametric equations. <br> 3. Define functions of several variables <br> 4. Define limits and continuity to function of two variables <br> 5. Generalize the techniques of single variable differential and integral calculus to two or <br> three variables; |  |

12. Student's obligation

- Attend and participate in lecture discussions
- Attend class prepared, ready to hand in homework and ready to work.
- Attend in exams


## 13. Forms of teaching

White board, Colorful markers, PowerPoint, data show.

## 14. Assessment scheme

Mid-course Exams 40\%
Final exam 60\%

## 15. Student learning outcome:

At the end of the course, all students will be able to do the following:

1. Find the angle between two vectors using the dot product
2. Find the cross product of two vectors in space
3. Write a set of parametric equations for a line in space
4. Find the distance between points, planes, and lines in space
5. Recognize and write equations for different surfaces
6. Sketch the graph and level curves of a function of two variables
7. Understand the limit, continuity, and differentiability of a function of two variables
8. Find partial derivative and higher-order partial derivatives of a function of two variables
9. Use the Chain Rule for functions of several variables
10. Find partial derivatives implicitly
11. Find and use directional derivatives and gradient of a function of two variables
12. Apply double integrals to represent the volume of a solid region and to find surface area

## 16. Course Reading List and References:

- Key references:

1. Thomas A., Calculus with Diff. Equation.11ed, Addison Wesley Pub. Comp., 2010
2. Adams R. \& Christopher E. , Calculus Several Variables. 7ed , Pearson Edu. Canada, 2010
-Useful references:
3. David B, Calculus Demystified, McGraw-Hill Comp., 2007
4. Stewart J, Essential Calculus early transcendentals, Bob Pirtle pub. Canada, 2007
5. Staley I. Grossman , Calculus .5ed , Saunders College Pub., 1997
6. Kaplan W. , Advanced Calculus .5ed , Addison Wesley Pub. Comp., 2000
7. Any other textbook in calculus or advance calculus

| 17. The Topics: | Lecturer's name |
| :--- | :--- |
| Course book \& Review | Week 1 |
| Three-dimensional Coordinate Systems | Week 2 |
| Length of the vector \& vector Algebra | Week 3 |

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| Dot Product | Week 4 |
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| Vector projection \& Cross Product. | Week 5 |
| Plane Curve (Curves and Parametric Equations) | Week 6 |
| Quadratic surface | Week 7 |
| Function of two variables (Domain \& range, graphs, level <br> curves) | Week 8 |
| Limits and Continuity in Higher Dimensions | Week 9 |
| Partial Derivatives | Week 10 |
| The Chain Rule | Week 11 |
| Directional Derivatives and Gradient Vectors, Tangent <br> Planes and Differentials | Week 12 |
| Extreme Values and Saddle Points | Week 13 |
| Implicit differentiation | Week 14 |

## 19. Examinations:

$\mathrm{Q} 1 /$ if $\mathrm{w}=e^{x y z}, \mathrm{x}=3 u+v, \mathrm{y}=3 u-v$ and $\mathrm{z}=u^{2} v$, find $\frac{\partial w}{\partial u}$ and $\frac{\partial w}{\partial v}$ using chain rule.

Q2/ Find direction derivative and gradient if $\quad f(x, y)=\ln \left(1+x^{2}+y\right)$
Q3/ Sketch the graph of $r=1+2 \cos \theta$, in polar coordinate.
Q4/ Find the distance and cosine between the vectors $\mathrm{v}=(1,-1,-2)$ and $\mathrm{u}=(-4,0,2)$, and prove that $\quad \cos \alpha^{2}+\cos \beta^{2}+\cos \gamma^{2}=1$.

## 20. Extra notes:

Here the lecturer shall write any note or comment that is not covered in this template and he/she wishes to enrich the course book with his/her valuable remarks.

## 21. Peer review

