

diff or Diff - differentiation or partial differentiation

$$\text{diff}(f, x_1, \dots, x_j) \quad \frac{d^j}{dx_1 \dots dx_j} f$$

$$\text{diff}(f, [x_1^n]) \quad \frac{d^n}{dx_1^n} f$$

$$\text{diff}(f, x_1^n, [x_2^n, x_3], \dots, x_j, [x_k^m]) \quad \frac{d^r}{dx_k^m dx_j \dots dx_3 dx_2^n dx_1^n} f$$

f - algebraic expression or an equation

x1, x2, ..., xj - names representing differentiation variables

n algebraic expression entering constructions like x^n, representing nth order derivative, assumed to be integer order differentiation

Find $\frac{d(x \sin(\cos x))}{dx}$

> diff(x*sin(cos(x)), x);

$$\sin(\cos(x)) - x \cos(\cos(x)) \sin(x)$$

Find higher order derivatives.

Find $\frac{d^3 \sin x}{dx^3}$

> diff(sin(x), x\$3);

$$-\cos(x)$$

Compute partial derivatives.

Ex: Find $\frac{\partial^2 (x^2 + x y^2)}{\partial y \partial x}$. > diff(x^2+x*y^2, x, y);

$$2y$$

The Diff command is inert, it returns unevaluated.

> Diff(tan(x), x);

$$\frac{d}{dx} \tan(x)$$

The command `map(f,list)` applies the function `f` to each element of the list.

Ex: To find third derivative of $\sin x$, $\tan x$ and $\cot^{-1}x$.

Sol: `> map(diff,[sin(x),tan(x), arccot(x)], x$3);`

$$\left[-\cos(x), 2(1 + \tan(x)^2)^2 + 4 \tan(x)^2 (1 + \tan(x)^2), -\frac{8x^2}{(1+x^2)^3} + \frac{2}{(1+x^2)^2} \right]$$

implicitdiff

- differentiation of a function defined by an equation

`implicitdiff(f, y, x)`

`f` algebraic expressions or equations

`y` (variable) name or function of dependent variable

`x` name (of derivative variable)

EX: find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ from $x^2+y^2=1$

Sol: `implicitdiff(x^2+y^2=1,y,x)`

Ex: Find $\frac{d^2y}{dx^2}$ if $x^2 + y^3 = 1$. Answer:

`> f := x^2 + y^3 = 1;`

`> implicitdiff(f, y, x, x);`

$$-\frac{2}{9} \frac{3y^3 + 4x^2}{y^5}$$

int - definite and indefinite integration

`int(expression,x, options)` $\int expression \, dx$

`int(expression,x=a..b, options)` $\int_a^b expression \, dx$

Double integration

`int(expression, [x, y], options)` $\iint expression \, dx \, dy$

`int(expression, [x = a..b, y = c..d], options)` $\int_c^d \int_a^b expression \, dx \, dy$

expression - algebraic expression; integrand

x, y - names; variables of integration

a, b, c, d - endpoints of interval on which integral is taken

options (optional) various options to control the type of integration performed.

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> *Int(f, x)*

$$\int f dx$$

> **v := Int(f(x), x = a..b);**

$$v := \int_a^b f(x) dx$$

Double integral

> *Int(f, x, y)*

$$\iint f dx dy$$

Triple integral

> *Int(f, x, y, z)*

$$\iiint f dx dy dz$$

Examples

> **int(x/(x^3-1), x);**

$$\frac{1}{3} \ln(x-1) - \frac{1}{6} \ln(x^2+x+1) + \frac{1}{3} \sqrt{3} \arctan\left(\frac{1}{3} (2x+1)\sqrt{3}\right)$$

> `int(exp(-x^2)*ln(x), x=0..infinity);`

$$-\frac{1}{4} \sqrt{\pi} \gamma - \frac{1}{2} \sqrt{\pi} \ln(2)$$

A double integral

> `int(x*y^2, [x, y]);`

$$\frac{1}{6} x^2 y^3$$

> `int(x*y^2, [x = 0..y, y = -2..2]);`

$$\frac{32}{5}$$

Find:

1) $\int_0^1 e^{x^3} dx$ > `f := int(exp(x^3), x = 0..1);`

$$f := \int_0^1 e^{x^3} dx$$

> `evalf(%)`

1.341904418

> `int(exp(x^3), x = 0..1, numeric)`

1.341904418

$$2) f := \int_a^b \frac{1}{x} dx$$

> `f := int(1/x, x = a..b);`

Warning, unable to determine if 0 is between a and b; try to use assumptions or use the AllSolutions option

$$f := \int_a^b \frac{1}{x} dx$$

$$> f := \text{int}\left(\frac{1}{x}, x = a..b, \text{allsolutions}\right)$$

f :=

$$\left\{ \begin{array}{l} \left\{ \begin{array}{l} \text{undefined} \\ \left(\left\{ \begin{array}{l} \infty \\ -\ln(a) \end{array} \right\} \begin{array}{l} a=0 \\ \text{otherwise} \end{array} \right) + \left(\left\{ \begin{array}{l} -\infty \\ \ln(b) \end{array} \right\} \begin{array}{l} b=0 \\ \text{otherwise} \end{array} \right) \end{array} \right. \quad \begin{array}{l} \text{And}(0 < b, a < 0) \\ \text{otherwise} \end{array} \quad a < b \\ 0 \quad b = a \\ - \left(\left(\left\{ \begin{array}{l} \text{undefined} \\ \left(\left\{ \begin{array}{l} \infty \\ -\ln(b) \end{array} \right\} \begin{array}{l} b=0 \\ \text{otherwise} \end{array} \right) + \left(\left\{ \begin{array}{l} -\infty \\ \ln(a) \end{array} \right\} \begin{array}{l} a=0 \\ \text{otherwise} \end{array} \right) \end{array} \right) \right. \quad \begin{array}{l} \text{And}(0 < a, b < 0) \\ \text{otherwise} \end{array} \quad b < a \end{array} \right.$$

$$3) \int_a^b \frac{1}{e^x} dx$$

$$> f := \text{int}\left(\frac{1}{\exp(x)}, x = a..b, \text{allsolutions}\right)$$

$$f := \begin{cases} (e^b - e^a) e^{-b-a} & a < b \\ 0 & b = a \\ (e^b - e^a) e^{-b-a} & b < a \end{cases}$$

4) Find integral of $\sin x$, $\tan x$ and $\ln x$ to each elements.

$$> \text{map}(\text{int}, [\sin(x), \tan(x), \ln(x)], x)$$

$$5) \int_0^1 e^{-x^2} \ln(x) dx$$

6) Find the third integral of $\cos 2x$, $\cot 3x$ and $\sin^{-1} 2x$ to each elements.

$$7) \int x e^{ax} \sin(bx) dx$$