Ministry of Higher Education \& Scientific Res.
Salahaddin University- Erbil
Collage of Science
Computer Science \& IT Department

Subject: Linear Algebra\& Statistic

## Class: $\mathbf{2}^{\text {nd }}$

## Q1) Answer the following:

a) A problem is given to three people $P, Q, R$ whose respective chances of solving it are $2 / 7,4 / 7,4 / 9$ respectively. What is the probability that the problem is solved?
b) Two die are rolled, find the probability that the sum is equal to 1 .
c) Tickets numbered $\mathbf{1}$ to $\mathbf{2 0}$ are mixed up and then a ticket is drawn at random. What is the probability that the ticket drawn has a number which is a multiple of 3 or 5 ?
d) Rotate $x=(4,2), \frac{\pi}{4}$ Counter-clockwise and then project on the $x$-axis.
e) Given $u=(3,-1,4)$ and $v=(2,0,1)$,then $(v \times u)=$ $\qquad$
Q2) Calculate Mean, Median, Mode for the following grouped data

| Class | Frequency |
| :---: | :---: |
| $10-12$ | 5 |
| $13-15$ | 8 |
| $16-18$ | 5 |
| $19-21$ | 10 |
| $22-24$ | 2 |

Q3) Consider the polynomials $p(x)=1+3 x+2 x^{2}, q(x)=x+3+2 x^{2}, r(x)=x^{2}+2 x$ in $P_{2}$, is $\{p(x), q(x), r(x)\}$ L.D or L.I ? Why?

Q4) Find all the Eigen values for the given matrix

$$
A=\left[\begin{array}{rrr}
\mathbf{1} & -\mathbf{1} & 0 \\
-1 & 2 & -1 \\
\mathbf{0} & -\mathbf{1} & 1
\end{array}\right]
$$

Q5)Prove that the set $V=M_{n \times n}$, which contains square matrix and $\left|M_{n \times n}\right|=0$ is not avector space .

Q 6)By Using Cramer's rule solve the following system of linear equation (using while loop) write program and results

$$
\begin{array}{r}
x+3 y-2 z=5 \\
3 x+5 y+6 z=7 \\
2 x+4 y+3 z=8
\end{array}
$$

Q7) Find root of function $f(x)=4 x e^{-x^{2}}-1$ using False position Method and Bisection method, in $\left[0, \frac{p i}{2}\right]$ and $\mathrm{e}=0.0001$, in which iteration the root appears? Write the result of last iteration. (use while ) don't use function inline .

Q8) Write program that evaluate the sum of diagonal elements of a matrix and multiply the result by 3 when the input matrix is square and its size is greater than 3.(using while loop)

Q9) Create a script file to generate ( N X N) matrix in form like using (while, if)
$\left[\begin{array}{lllll}\mathbf{1} & 0 & \mathbf{1} & 0 & \mathbf{1} \\ 0 & \mathbf{1} & 0 & \mathbf{1} & 0 \\ \mathbf{1} & 0 & \mathbf{1} & 0 & \mathbf{1} \\ 0 & \mathbf{1} & 0 & \mathbf{1} & 0 \\ \mathbf{1} & 0 & \mathbf{1} & 0 & \mathbf{1}\end{array}\right]$

Q10) Write a program to find $\cos \theta$ for any two vectors, don't forget the norm should be positive ,then check if the vectors are orthogonal or not.

Q11) Write a Matlab program with

- input parameters A, a matrix,
and $n$, an integer,
- output parameter $p$ where $p=-1$ if there is no column $n$ in $A$; otherwise $p$ is the maximum absolute value in column $n$ of $A$

Q12) write program to evaluate the value of $\boldsymbol{e}^{\boldsymbol{x}}$, using while

$$
e^{x}=1+x+\frac{x^{2}}{2!}+\frac{x^{3}}{3!}+\cdots+\frac{x^{n}}{n!}+\ldots
$$

Q13) Write a program to display the multiplication table , using while.
Q14) let Grades are to be assigned as follows:
A 80\%-100\%
B 65\%-79\%
C 50\%-64\%.
Write a script file to input a mark for 4 students and display the appropriate grade. If the user enters a number greater than 100 or less than zero, display that the mark is invalid.

Q15) write matlab program that evaluate the sum of series below

$$
\operatorname{sum}=\sum_{i=1}^{n} \frac{(-1)^{i-1} x^{2 i-1}}{(2 i-1)!}
$$

Q16) Write program that evaluate the sum of first row of matrix and multiply the result by 3 when the input matrix is square and its sum of diagonal elements are equal to zero.(using while loop)

Q17) Using a for loop to investigate the following consider all possible outputs, when $x$ is from -6 to 8 in increments of 0.5 , Also display how many answers are greater than 5

$$
f(x)=\left\{\begin{array}{lr}
(6+x) & x<0 \\
(x-2)+2 & 0 \leq x \leq 4 \\
\frac{x^{2}}{x+1}+3 e^{-4 x} \cos 5 x-\left(\frac{2 e^{-3 x}}{\sin 2 x}\right) & x>4
\end{array}\right.
$$

