Ministry of Higher Education & Scientific Research

Salahaddin University-Erbil

College of Administration and Economics

Statistics & Informatics Department

Fourth Year Stage (Senior)

QUESTIONS BANK OF MULTIVARIATE STATISTICAL ANALYSIS

Q1/ Are the following statements TRUE or FALSE? Correct the false statements?

- 1) In multivariate statistical analysis, the word "multivariate" indicates that in a single analysis two dependent variables are simultaneously used.
- 2) X_{jk} = The jth item for the measurement of the kth variable.
- 3) Comparing the means of the weight, length, and blood sugar level variables for people in Iraq, France, Japan, and Iran is an example of analysis of variance (ANOVA).
- 4) (ABC)' = A' B'C'
- 5) When $A^{-1} = A'$, A is called Idempotent matrix.

6) If
$$\mathbf{A} = \begin{bmatrix} 1 & 0 & 4 \\ 0 & 5 & 9 \\ 4 & 9 & -1 \end{bmatrix}$$
 and let $\mathbf{C} = \begin{bmatrix} 2 & 0 & 4 \\ 2 & 1 & 4 \\ 3 & 1 & 4 \end{bmatrix}$, then $tr(C^{-1}AC) = 5$

7) Let
$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 5 & 9 \\ 0 & 9 & -1 \end{bmatrix}$$
 and $\underline{X} = \begin{bmatrix} X_1 \\ X_2 \\ X_3 \end{bmatrix}$. Then, quadratic form $Q(\underline{X}) = x_1^2 + 9x_1x_2 + 5x_2^2 + 2x_3^2$

8) If
$$\underline{X} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$
 and $A = \begin{bmatrix} 4 & -1 \\ -1 & 4 \end{bmatrix}$, then $Q(\underline{X})$ is p.s.d.

9) If
$$A = \begin{bmatrix} -7 & 0 \\ 0 & 7 \end{bmatrix}$$
, then $Q(\underline{X})$ is p.d.

10) If
$$\underline{X}^{(1)}$$
, $\underline{X}^{(2)}$ are dependent, then $E\left(\underline{X}^{(1)} - \underline{\mu}^{(1)}\right)\left(\underline{X}^{(2)} - \underline{\mu}^{(2)}\right)' = \mathbf{0}$

- 11) In multivariate statistical analysis, the word "multivariate" indicates that two or more dependent variables are simultaneously used in a single analysis.
- 12) Correlation for multiple regression predictions always infers causation.
- 13) The higher the multicollinearity, the smaller the standard error for the regression coefficients.
- 14) Data errors and observations which represent extreme magnitudes on variables are both causes of outliers.

Q2/ For the following data that are normally distributed $(\underline{X} \sim N(\underline{\mu}, \Sigma))$, find X matrix, mean vector, var-covar matrix, and prove or disprove that $\underline{X}^{(1)}$ and $\underline{X}^{(2)}$ are independent, if:

$\underline{X}^{(1)} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}, \underline{X}^{(2)} = \begin{bmatrix} x_3 \end{bmatrix}$						
X 1	1	2	3	4	5	
X 2	5	4	3	2	1	
Х3	-2	-2	-2	-2	-2	

Q3/ Let
$$\underline{X} \sim N(\underline{\mu}, \Sigma)$$
, where $\underline{X} = \begin{bmatrix} \underline{X}^{(1)} \\ \underline{X}^{(2)} \end{bmatrix}$, $\Sigma = \begin{bmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{bmatrix}$

If $\underline{X}^{(1)}$ and $\underline{X}^{(2)}$ are independent. Show that $\sum_{12} = 0$

Q4/ If the quadratic form $Q(\underline{X}) = 2x_1^2 + 4x_3^2 + 2x_1x_2 + 6x_2x_3 + 5x_4^2 + 7x_1x_3$

Find:

- 1. The matrix A,
- 2. What is the classification of Q(X) and why? (p.d., p.s.d, n.d., n.s.d)

Q5/ Multiple choices: Select the best answer for the following statements:

* _	. used when a numerical predictor has a curvilinear relationship with the response.						
	a. Simple regression	b. Multiple regression	c. Quadratic regression				
	d. all of them	e. None of them					
* _	❖ used to check the assumptions of the regression model.						
	a. Stepwise regression	b. R ² Adjusted c.	Correlation				
	d. all of them	e. None of them					
worst kind of outlier, can totally reverse the direction of association between x and y.							
	a. Residual plots	b. independent variable	c. dependent variable				
	d. bar chart	e. None of them					
problem that can occur when the information provided by several predictors overlaps.							
	a. Cause and effect	b. Logistic regression	c. Factor analysis				
	d. Error	e. None of them					
 Q6/ Fill the blanks for the following statements: ✓ The most popular rotation strategy in factor analysis is ✓ is a correlational technique that allows you to evaluate the relationship between two variables with the effects of a third removed from both of them. ✓ The number of possible discriminant functions in a discriminant analysis is limited to or to, whichever is less. ✓ In the formula for the Pearson correlation coefficient, the calculation of variability can be found in 							
Q7/ For every vector $\underline{\alpha}$ if $\underline{X}^{(1)}$ and $\underline{X}^{(2)}$ are independent. Let X_i be any Component of $\underline{X}^{(1)}$, Show That for all linear Combination $\underline{\alpha} \underline{X}^{(2)}$ Which is Minimize the Variance $(X_i - \underline{\alpha} \underline{X}^{(2)})$.							
Q8/ If we have three Variables (p=3), $R_{1.23}^2 = \frac{\rho_{12}^2 + \rho_{13}^2 - 2\rho_{12}\rho_{13}\rho_{23}}{(1-\rho_{23}^2)}$, and $\rho_{13.2}^2 = \left(\frac{\rho_{13} - \rho_{12}\rho_{23}}{\sqrt{1-\rho_{12}^2}\sqrt{1-\rho_{23}^2}}\right)^2$. Prove that $1 - R_{1.23}^2 = (1 - \rho_{12}^2)(1 - \rho_{13.2}^2)$							