

Ministry of Higher Education & Scientific Research
 Salahaddin University-Erbil
 College of Administration and Economics
 Statistics & Informatics Department
 Fourth Year Stage (Senior)

QUESTIONS BANK OF MULTIVARIATE STATISTICAL ANALYSIS

Q1/ Are the following statements TRUE or FALSE? Correct the false statements?

- 1) In multivariate statistical analysis, the word “multivariate” indicates that in a single analysis two dependent variables are simultaneously used.
- 2) X_{jk} = The j^{th} item for the measurement of the k^{th} variable.
- 3) Comparing the means of the weight, length, and blood sugar level variables for people in Iraq, France, Japan, and Iran is an example of analysis of variance (ANOVA).
- 4) $(ABC)' = A' B' C'$
- 5) When $A^{-1} = A'$, A is called Idempotent matrix.
- 6) If $A = \begin{bmatrix} 1 & 0 & 4 \\ 0 & 5 & 9 \\ 4 & 9 & -1 \end{bmatrix}$ and let $C = \begin{bmatrix} 2 & 0 & 4 \\ 2 & 1 & 4 \\ 3 & 1 & 4 \end{bmatrix}$, then $tr(C^{-1}AC) = 5$
- 7) Let $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 5 & 9 \\ 0 & 9 & -1 \end{bmatrix}$ and $\underline{X} = \begin{bmatrix} X_1 \\ X_2 \\ X_3 \end{bmatrix}$. Then, quadratic form $Q(\underline{X}) = x_1^2 + 9x_1x_2 + 5x_2^2 + 2x_3^2$
- 8) If $\underline{X} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$ and $A = \begin{bmatrix} 4 & -1 \\ -1 & 4 \end{bmatrix}$, then $Q(\underline{X})$ is p.s.d.
- 9) If $A = \begin{bmatrix} -7 & 0 \\ 0 & 7 \end{bmatrix}$, then $Q(\underline{X})$ is p.d.
- 10) If $\underline{X}^{(1)}, \underline{X}^{(2)}$ are dependent, then $E \left(\underline{X}^{(1)} - \underline{\mu}^{(1)} \right) \left(\underline{X}^{(2)} - \underline{\mu}^{(2)} \right)' = \mathbf{0}$
- 11) In multivariate statistical analysis, the word “multivariate” indicates that two or more dependent variables are simultaneously used in a single analysis.
- 12) Correlation for multiple regression predictions always infers causation.
- 13) The higher the multicollinearity, the smaller the standard error for the regression coefficients.
- 14) Data errors and observations which represent extreme magnitudes on variables are both causes of outliers.

Q2/ For the following data that are normally distributed ($\underline{X} \sim N(\underline{\mu}, \Sigma)$), find X matrix, mean vector, var-covar matrix, and prove or disprove that $\underline{X}^{(1)}$ and $\underline{X}^{(2)}$ are independent, if:

$$\underline{X}^{(1)} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}, \underline{X}^{(2)} = [x_3]$$

x_1	1	2	3	4	5
x_2	5	4	3	2	1
x_3	-2	-2	-2	-2	-2

Q3/ Let $\underline{X} \sim N(\underline{\mu}, \Sigma)$, where $\underline{X} = \begin{bmatrix} \underline{X}^{(1)} \\ \underline{X}^{(2)} \end{bmatrix}$, $\Sigma = \begin{bmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{bmatrix}$

If $\underline{X}^{(1)}$ and $\underline{X}^{(2)}$ are independent. Show that $\Sigma_{12} = 0$

Q4/ If the quadratic form $Q(\underline{X}) = 2x_1^2 + 4x_3^2 + 2x_1x_2 + 6x_2x_3 + 5x_4^2 + 7x_1x_3$

Find:

1. The matrix A,
2. What is the classification of $Q(\underline{X})$ and why? (p.d., p.s.d, n.d., n.s.d)

Q5/ Multiple choices: Select the best answer for the following statements:

- ❖ ___ used when a numerical predictor has a curvilinear relationship with the response.
 - a. Simple regression
 - b. Multiple regression
 - c. Quadratic regression
 - d. all of them
 - e. None of them
- ❖ ___ used to check the assumptions of the regression model.
 - a. Stepwise regression
 - b. R^2 Adjusted
 - c. Correlation
 - d. all of them
 - e. None of them
- ❖ ___ worst kind of outlier, can totally reverse the direction of association between x and y.
 - a. Residual plots
 - b. independent variable
 - c. dependent variable
 - d. bar chart
 - e. None of them
- ❖ ___ problem that can occur when the information provided by several predictors overlaps.
 - a. Cause and effect
 - b. Logistic regression
 - c. Factor analysis
 - d. Error
 - e. None of them

Q6/ Fill the blanks for the following statements:

- ✓ The most popular rotation strategy in factor analysis is _____.
- ✓ _____ is a correlational technique that allows you to evaluate the relationship between two variables with the effects of a third removed from both of them.
- ✓ The number of possible discriminant functions in a discriminant analysis is limited to _____ or to _____, whichever is less.
- ✓ In the formula for the Pearson correlation coefficient, the calculation of variability can be found in _____

Q7/ For every vector $\underline{\alpha}$ if $\underline{X}^{(1)}$ and $\underline{X}^{(2)}$ are independent. Let X_i be any Component of $\underline{X}^{(1)}$, Show That for all linear Combination $\underline{\alpha} \underline{X}^{(2)}$ Which is Minimize the Variance $(X_i - \underline{\alpha} \underline{X}^{(2)})$.

Q8/ If we have three Variables ($p=3$), $R_{1.23}^2 = \frac{\rho_{12}^2 + \rho_{13}^2 - 2\rho_{12}\rho_{13}\rho_{23}}{(1 - \rho_{23}^2)}$, and $\rho_{13.2}^2 = \left(\frac{\rho_{13} - \rho_{12}\rho_{23}}{\sqrt{1 - \rho_{12}^2}\sqrt{1 - \rho_{23}^2}} \right)^2$.
 Prove that $1 - R_{1.23}^2 = (1 - \rho_{12}^2)(1 - \rho_{13.2}^2)$