Ministry of Higher Education & Scientific Research



# **Department of Mathematics**

**College of Science** 

# **University of Salahaddin-Erbil**

**Subject:** Number Theory

## **Course Book: 4<sup>th</sup> year students**

Lecturer's Name: Prof. Herish O. Abdullah

Academic Year: 2024/2025

# **Course Book**

1. Course name	Number Theory	
2. Lecturer in charge	Herish O. Abdullah	
3. Department/ College	Mathematics, College of Science	
<b>4. Contact</b> Email:	herish.abdullah@su.edu.krd	
Tel:	0750 455 0470	
5. Time (in hours) per week	3/Group	
6. Office hours	Sunday 10:30-12:30 am	
7. Course code		
8. Teacher's academic profile	Dr. Herish Omer Abdullah is a Professor in the Department of	
	Mathematics at the College of Science, Salahaddin University-	
	Erbil. He completed his Ph.D. in Graph Theory at the same	
	institution in 2007, with a thesis titled "Hosoya Polynomials of	
	Steiner Distance of Some Graphs." He holds an M.Sc. in Applied	
	Algebra (Group Representation Theory) from the University of	
	Technology-Baghdad, earned in 1998, and a B.Sc. in Mathematics	
	from Salahaddin University-Erbil, awarded in 1991.	
9. Keywords	Graph Theory, topological indices of graphs, authentication	

#### 10. Course overview:

This course provides an introduction to the important basic topics of number theory: prime numbers, factorization, congruence and representation of numbers, Quadratic Residues and Reciprocity and Diophantine equations.

#### 11. Course objective:

To give the students an introduction to basics of number theory. On successful completion of the course students will be able to:

1. Explain some of the concepts of number theory, a primary area of mathematics, using examples.

2. Apply mathematical ideas and concepts within the context of number theory.

3. Solve a range of problems in number theory.

#### 12. Student's obligation:

In their academic year, students are obliged to take exams, do assignment and quizzes. There will be optional projects and programming assignments, which may add extra marks to the students overall performance.

#### 13. Forms of teaching:

The lectures are taught through projector and whiteboard.

#### 14. Assessment scheme:

Assessed works include midterm exam(s), quizzes, optional projects, final exam related to the materials studied.

#### **Distribution of marks:**

Midterm exam: 20% Quizzes: 10% Class assignments, homework & reports: 10% Final exam: 60% marks

#### **15. Student learning outcome:**

#### 16. Recommended Course Reading List and References:

Directorate of Quality Assurance and Accreditation بەر يو متمانەبەخشىن كانىيايى جۆرى و متمانەبەخشىن

Joseph H. Silverman, a Friendly introduction to Number Theory, (Fourth Edition), 2012.		
Titu Andreescu, Dorin Andrica, Number Theory, Structures, Examples, and Problems (2009).		
17. The Topics:	Lecturer's name	
Weekly Topics:	Prof Dr Herish O	
Introduction:	Abdullah	
Historical overview and significance of number theory		
Divisibility and prime numbers		
The Fundamental Theorem of Arithmetic		
Congruences and Modular Arithmetic:		
Modular arithmetic operations		
Congruence relations and properties		
Solving linear Congruences		
Chinese Remainder Theorem		
Linear Diophantine equations		
Pythagorean triples		
Fermat's Last Theorem (statement and historical background)		
Arithmetic Functions:		
Euler's totient function		
Möbius function		
Summation formulas (e.g., divisor function, sum of squares)		
Quadratic Residues:		
Quadratic residues and non-residues		
Fuler's criterion		
Quadratic reciprocity theorem		
Prime Number Factorization (Optional)		
Prime distribution and prime counting functions		
Prime factorization methods: Trial division, Pollard's rho algorithm		
The Sieve of Eratosthenes and its role in prime factorization		
The Fundamental Theorem of Arithmetic and unique factorization		
Factoring large composite numbers: Fermat's factorization method.		
Quadratic Sieve, General Number Field Sieve (GNFS)		
Primality testing vs. factorization		
18. Practical Tonics (If there is any)		
19. Examinations:		
20. Extra notes:		

### ينداچوونهوه هاوه فل 21. Peer review

This course book has to be reviewed and signed by a peer. The peer approves the contents of your course book by writing few sentences in this section.

(A peer is person who has enough knowledge about the subject you are teaching, he/she has to be a professor, assistant professor, a lecturer or an expert in the field of your subject).

ئەم كۆرسىبووكە دەبنىت لەلايەن ھاوملْنِكْى ئەكادىمىيەۋە سەير بكرنىت و ناو مرۆكى بابەتەكانى كۆرسەكە پەسەّند بكات و جەند ووشەييەڭ بنووسنىت لەسەر شياوى ناوەرۆكى كۆرسەكە و واژووى لەسەر بكات.

هاوه ل ئمو كمسميه كه زانياري همبنت لمسمر كۆرسىمكە و دەبيت پلمى زانستى له مامۆستا كەمتر نمبنت.