Salahaddin University-Erbil
College of Science-Department of Mathematics

## Question Bank about

Numerical Analysis
$3^{\text {rd }}$ Year Second Semester
2023-2024

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Question 1: Prove that $\Delta(f(x)+g(x))=\Delta f(x)+\Delta g(x)$ that is $\Delta$ is distributive.

Question 2: If c is a constant then prove that $\Delta \mathrm{cf}(\mathrm{x})=\mathrm{c} \Delta \mathrm{f}(\mathrm{x})$.

Question 3: Find $f(12)$ from the following date by using backward difference

| $x$ | $F(x)$ |
| :--- | :--- |
| 1 | 1 |
| 10 | 4 |
| 15 | 7 |
| 20 | 10 |
| 25 | 12 |

Question 4: Use the Lagrange interpolation polynomial to find the value of $y$ at $x=2$ for the given set of points (1,2),(3, 4)

Question 5: Find the value of $y$ at $x=1$ for the given set of points $(1,6),(3,4),(2,5)$ use Lagrange interpolation.

Question 6: Fit the straight line to the following data by using least square method

| $X$ | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $Y$ | 1 | 2 | 3 | 4 | 5 |

a) $y=x$
b) $y=x+1$
c) $y=2 x$
d) $y=2 x+1$

Question 7: Fit the straight line curve to the following data.

| $x$ | 75 | 80 | 83 | 90 | 94 | 98 | 100 | 102 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ | 30 | 34 | 67 | 46 | 28 | 87 | 23 | 54 |

a) $y=0.9288 x+7.78155$
b) $y=7.78155 x+0.9288$
c) $y=0.8288 x+6.78155$
d) $y=6.78155 x+0.8288$
and
a) $y=-0.2673 x^{2}+3.5232 x-0.9286$
b) $y=0.2673 x^{2}+3.5232 x-0.9286$
c) $y=0.2673 x^{2}+3.5232 x+0.9286$
d) $y=-0.2673 x^{2}+3.5232 x+0.9286$

Question 8: What constant c makes the expression $\sum_{k=0}^{n}\left|f\left(x_{k}\right)-c e^{x_{k}}\right|^{2}$ as small as possible?

Question 9: A physics process can be described with the equation $y=f(x)=\frac{a_{0}}{x}+\frac{a_{1}}{x^{2}}$. The measured value of $(x, y)$ are listed in the following table:

| $x$ | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- |
| $y$ | 3 | 0.9 | 0.6 | 0.4 |

Use direct nonlinear regression method to determine $a_{0}$ and $a_{1}$.

Question 10: Use least squares regression to fit a straight line to the data given. Along with the slope and intercept, compute the standard error of the estimate and the coefficient of determinant.

| X | 0 | 2 | 4 | 6 | 9 | 11 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 5 | 6 | 7 | 6 | 9 | 8 |

