

MEASURES OF CENTRAL TENDENCY (location):

- ⊕ A *measure of central tendency* is a descriptive statistic that describes the average, or typical value of a set of scores
- ⊕ There are three common measures of central tendency:
 - ✓ Arithmetic mean (A.M.): it is the ratio between the sum of variables and total number of observations.
 - ✓ Mode
 - ✓ Median

Other measures of central tendency are

1. Geometric Mean (G.M.)
2. Harmonic Mean (H.M.)
3. Weighted Mean (W.M.)

The most important types of mean are:

- ✓ Arithmetic mean (\bar{X})
 - For ungrouped data:
 - Sample: $\bar{X} = (\sum x_i)/n = x_1 + x_2 + x_3 + \dots + x_n/n$
 - Population: $\mu = (\sum x_i)/N = x_1 + x_2 + x_3 + \dots + x_n/N$
 - Grouped data:
 - Sample: $\bar{X} = \sum f_i x_i/n$
 - Population: $\mu = \sum f_i x_i/N$ $N = \sum f$

Example: from the following information calculate the mean of marks for (5) students in statistic.

Students	1	2	3	4	5
Marks (x_i)	95	70	75	90	82

$$\bar{X} = (\sum x_i)/n = x_1 + x_2 + x_3 + \dots + x_n/n$$

$$= (95 + 70 + 75 + 90 + 82)/5 = 82.4$$

Averages from Grouped Data

Frequency Distribution

No. of plants (X)	1	2	3	4	5
No. of flowers (f)	11	10	5	3	1

X	f	fX
1	11	11
2	10	20
3	5	15
4	3	12
5	1	5

$$\Sigma fi = 30 \quad \Sigma fi xi = 63 \quad \longrightarrow \quad \bar{X} = \Sigma fi xi / n = 63 / 30 = 2.1$$

Grouped Frequency Distribution

The lengths of 32 leaves were measured correct to the nearest mm. Find the mean length.

Length (mm)	20–22	23–25	26–28	29–31	32–34
Frequency	3	6	12	9	2

Length (mm)	Class mark (X_j)	f	$f_j X_j$
20–22	21	3	63
23–25	24	6	144
26–28	27	12	324
29–31	30	9	270
32–34	33	2	66

$$\Sigma fi = 32 \quad \Sigma fi xi = 867$$

$$\bar{X} = \Sigma fix_i / n = 867 / 32 = 27.1 \text{ mm}$$

- ✓ Mode (M_o): it is a datum which repeated more than others.
The mode may be:
- One datum
 - More than one datum
 - No mode

Example: The following data are the random height of 6 plants (cm):

1. 60, 65, 80, 70, 80, 80
2. 69, 50, 73, 54, 69, 73
3. 60, 63, 80, 70, 65, 50

- ✓ Median (M_e): is the value of datum which location at the middle of data after arranging them.

For calculating median we must:

1. Arrange the data from the lower value to the upper value or from upper to lower.
2. Limiting the Median value by one of these equations :
A/Median series = $(n+1)/2$ (in case of odd numbers)

Example: If the CaCO_3 % off (11) soil samples of were {20,23,30,24,25,26,27,29,30,21 and 20} , calculate median value.

1-Sample size =11

2-Data after arrangement: 20, 20, 21, 23, 24, 25, 26, 27, 29,30, 30.

3-Median series is $(11+1)/2 =6$

4-The Median value (M_e) =25

B/ Median series = $n/2$ and $(n/2)+1$,(in case of even number)

Example: If the number of apple /tree for 10 trees are :

30, 24, 34, 29, 40, 38, 50, 46, 52 and 52

Find the Median.

24,29,30, 34, 38, 40, 46, 50, 52, 52

Median series are : $n/2 = 10/2 = 5$

And $(n/2)+1 = (10/2) + 1 = 6$

Median value = $(38+40)/2 = 39$

➤ Geometric Mean (G.M.)

$$G.M = \sqrt[n]{x_1 x_2 x_3 \dots x_n}$$

- It is useful for averaging ratios and percentages rates are increase or decrease.

Example: The average person's monthly salary in a company jumped from \$2,500 to \$5,000 over the course of ten years. Using the geometric mean, what is the average yearly increase?

$$G.M = \sqrt[n]{x_1 x_2 x_3 \dots x_n}$$

$= \sqrt[10]{2500 * 5000} = 3535.53/10 = 353.53$ is average increase over ten years (according to the G.M).

➤ Harmonic Mean (H.M.)

- The harmonic mean is a very specific type of average
- It's generally used when dealing with averages of units, like speed, time or other rates such as km/hour, km/litre, etc.
- It can be computed when one or more items are zero

$$H.M = \frac{n}{\sum 1/x_i}$$

Example: Ali drives a car at 20 mph for the first hour and 30 mph for the second. What's his average speed?

$$\text{H.M} = \frac{n}{\sum 1/x_i} = 2 / (1/20) + (1/30) = 2 / (0.05 + 0.033)$$

$$= 24.09 \text{ mph or miles/hour}$$

➤ Weighted Mean:

$$\bar{X}_w = \frac{\sum X_i w_i}{\sum w_i}$$

Example: the following data represent a student marks of the first course:

Subject	marks (X_i)	unit (w_i)	$X_i w_i$
Statistics	93	3	93*3=279
Computer	90	2	90*2=180
English	87	2	87*2=154
		$\sum w_i = 7$	$\sum X_i w_i = 613$

$$\bar{X}_w = \frac{\sum X_i w_i}{\sum w_i} = 613/7 = 87.57$$