# Engineering Analysis 

Lec. 4
Fall course 2021-2022
$3^{\text {rd }}$ Year
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## Randomness and probability

## Objectives :

- Review a programming concept central by OOP.
- The random walker will serve as a template for how to moving objects around a Processing window.


## Random Walks

- An object in Processing is an entity that has both data and functionality.
- A class is the template for building actual instances of objects.

Let's begin by defining the Walker class, what it means to be a Walker object. Have $\mathrm{x}, \mathrm{y}$ location.
class Walker \{ int x ;
int $y$;
Also must contains constructor .

- a constructor special function that is called when the object is first created.

Walker() \{

$$
\begin{aligned}
& \mathrm{x}=\text { width } / 2 \\
& \mathrm{y}=\text { height } / 2
\end{aligned}
$$

## // initialize first location in the <br> // center of window

- Walker class has two functions:
first function that allows the object to display itself (as a white or black dot).
void render() \{
stroke(0); point(x,y);
\}

Second function directs the Walker object to take a step.
There are four possible steps. $\mathrm{X}++, \mathrm{X}--, \mathrm{Y}++, \mathrm{Y}-$
,By randomly pick from four choices using random(). void step() \{
int choice $=$ int(random(4));

```
if (choice == 0) {
//The random "choice" determines our step.
x++;}
else if (choice == 1) {
    x--;}
else if (choice == 2) {
y++;}
else {
        y--;}
}
}
in the main part of our sketch declare one global variable of type Walker.
Walker w;
Then create the new object and setup window size and color
    void setup() {
    size(640,360);
    w = new Walker(); Create the Walker.
    background(255);
    }
```

void draw() \{

## // Run the walker object

w.step();
w.render();
\}
This Walker's step choices are limited to four options-up, down, left, and right. But any given pixel in the window has eight possible neighbors, and a ninth possibility is to stay in the same place.


4 possible steps


8 possible steps

## Randomly step to eight possible neighbors

```
void step() {
int stepx = int(random(3))-1; //Yields -1, 0, or 1
int stepy = int(random(3))-1;
x += stepx;
y += stepy;
}
```

Probability of four neighbor step $=\frac{1}{4}=25 \%$ chance
Probability of eight neighbor or remaining in its location $=\frac{1}{9}=11 \%$ chance

## Probability and Non-Uniform Distributions

With a few tricks, we can change the way to use random() to produce "non-uniform" distributions of random numbers.by many ways:

First: fill an array with a selection of numbers-some of which are repeated then choose random numbers from that array and generate events based on those choices.

```
int[] stuff = new int[5];
stuff[0] = 1;
stuff[1] = 1; // probability to pick 1 will be 40%
stuff[2] = 2; // probability to pick 2 will be 20%
stuff[3] = 3; // probability to pick 3 will be 40%
stuff[4] =3;
int index = int(random(stuff.length)); //Picking a random element from an array
```

Second : allow an event to occur only if our random number is within a certain range. Example: Let's say that Outcome A has a 60\% chance of happening, Outcome B has 10\% chance, and Outcome C, a $30 \%$ chance.
$>$ between 0.00 and 0.60 (60\%) $->$ Outcome A
$>$ between 0.60 and 0.70 (10\%) -> Outcome B
$>$ between 0.70 and 1.00 (30\%) -> Outcome C

```
Sol.
float num = random(1);
if (num < 0.6) {
    println("Outcome A");
} else if (num < 0.7) {
    println("Outcome B");
} else {
    println("Outcome C");
}
```

We could use the above methodology to create a random walker that tends to move to the right. Here is an example of a Walker with the following probabilities:
$>$ chance of moving up: 20\%
$>$ chance of moving down: 20\%
$>$ chance of moving left: 20\%
$>$ chance of moving right: $40 \%$

```
void step() {
float r = random(1);
if (r<0.4) { //40% chance of moving to the right!
x++;
} else if (r < 0.6) {
x--;
} else if (r<0.8) {
y++;
} else {
y--;}
}
```


## Exercise

Create a random walker with dynamic probabilities. As instance you can give it a $50 \%$ chance of moving in the direction of the mouse?

