Salahaddin University-Erbil
College of Administration and Economics Department: Statistics and Information $2^{\text {nd }}$ Examination


Subject: Experimental Design
Date: 12-4-2022
Stage: four
Time: 90 minutes

Q1// A) Create the design for:
(10 Marks)
1- GLS with 4 replications.

1. CRD $(2 \times 3 \times 2)$ with 2 replications.
B) Create the Linear Model for:
(10 Marks)
2. $\operatorname{RCBD}(9 \times 3 \times 5) \mathrm{r}=6$.
3. CRD $(9 \times 4)$ with 5 replications.

Q2// from the following data Factorial (RCBD) test if there are any deferent or not? $a=5 \%$
(40 Marks)

|  | $\mathrm{b}_{1}$ |  | $\mathrm{~b}_{2}$ |  | $\mathrm{~b}_{3}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{a}_{1}$ | $\mathrm{a}_{2}$ | $\mathrm{a}_{1}$ | $\mathrm{a}_{2}$ | $\mathrm{a}_{1}$ | $\mathrm{a}_{2}$ |
| r 1 | $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{9}$ | $\mathbf{8}$ | $\mathbf{1}$ | $\mathbf{2}$ |
| r 2 | $\mathbf{5}$ | $\mathbf{2}$ | $\mathbf{1 0}$ | $\mathbf{9}$ | $\mathbf{3}$ | $\mathbf{4}$ |

$\mathrm{Q} 3 / /$ from Q 2 find $\mathrm{LSD}_{a}$ (least significant deference)
(40 Marks)
$\mathbf{F}_{(0.05 ; 5,1)}=230.1619, \mathbf{F}_{(\mathbf{0 . 0 5 ; 1 , 5})}=6.6079, \mathbf{F}_{(0.01 ; 1,5)}=16.2582, \mathbf{F}_{(0.05 ; 2,5)}=5.7861, \mathbf{t}_{(0.025 ; 5)}=2.571, \mathbf{t}_{(0.05 ; 5)}=2.015$

## Good Luck



Dr. Omiad Saber Abdullah Shwany

Salahaddin University-Erbil
College of Administration and Economics
Department: Statistics and Information
$2^{\text {nd }}$ Examination

Subject: Experimental Design
Date: 12-4-2022
Stage: four
Time: $\underline{\mathbf{0}}$ minutes

Q1// A) Create the design for:
(10 Marks)
2- GLS with 4 replications.

1. CRD $(2 \times 3 \times 2)$ with 2 replications.
B) Create the Linear Model for:
2. $\operatorname{RCBD}(9 \times 3 \times 5) \mathrm{r}=6$.
3. $\mathrm{CRD}(9 \times 4)$ with 5 replications.

Q2// from the following data Factorial (RCBD) test if there are any deferent or not? $a=5 \%$
(40 Marks)

|  | $\mathrm{b}_{1}$ |  | $\mathrm{~b}_{2}$ |  | $\mathrm{~b}_{3}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{a}_{1}$ | $\mathrm{a}_{2}$ | $\mathrm{a}_{1}$ | $\mathrm{a}_{2}$ | $\mathrm{a}_{1}$ | $\mathrm{a}_{2}$ |
| r1 | $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{9}$ | $\mathbf{8}$ | $\mathbf{1}$ | $\mathbf{2}$ |
| r2 | $\mathbf{5}$ | $\mathbf{2}$ | $\mathbf{1 0}$ | $\mathbf{9}$ | $\mathbf{3}$ | $\mathbf{4}$ |

Q3// from Q2 find $\mathrm{LSD}_{a}$ (least significant deference)
(40 Marks)
$\mathbf{F}_{(0.05 ; 5,1)}=230.1619, \mathbf{F}_{(0.05 ; 1,5)}=6.6079, \mathbf{F}_{(0.01 ; 1,5)}=16.2582, \mathbf{F}_{(0.05 ; 2,5)}=5.7861, \mathbf{t}_{(0.025 ; 5)}=2.571, \mathbf{t}_{(0.05 ; 5)}=2.015$

## Good Luck



Dr. Omiad Saber Abdullah Shwany

Salahaddin University-Erbil
College of Administration and Economics
Department: Statistics and Information
Final Exam: $1^{\text {st }}$ Trial 2021-2022

Subject: Experimental Design
Date: 21-5-2022 Saturday
Stage: four
Time: 3 Hours

Q1// from the following data test if there are any deferent or not? if the experimental unit are homogeneous?
With five stapes, alpha $=0.05$ :
(20 Marks)

| $\mathrm{T}_{\text {emperature }}$ | $\mathrm{R}_{\text {eplications }}$ | Pressure |  |  | Sum Ai |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{b}_{1}=200$ | $\mathrm{b}_{2}=215$ | $\mathrm{b}_{3}=230$ |  |  |
| $a_{1}=150$ | $\mathrm{r}_{1}$ | 90.4 | 90.7 | 90.2 | 542.5 | if : |
|  | $\mathrm{r}_{2}$ | 90.2 | 90.6 | 90.4 |  | $\mathrm{F}_{(0.05 ; 3 ; 6)}=4.7571$ |
| $\mathrm{a}_{2}=160$ | $\mathrm{r}_{1}$ | 90.1 | 90.5 | 89.9 | 541.5 | $\mathrm{F}_{(0.05 ; 6 ; 3)}=8.9407$ |
|  | $\mathrm{r}_{2}$ | 90.3 | 90.6 | 90.1 |  | $\mathrm{F}_{(0.05 ; 2,9)}=4.2565$ |
|  | I |  |  |  |  | $\mathrm{F}_{(0.05 ; 4,9)}=3.6331$ |
| $\mathrm{a}_{3}=170$ | $\mathrm{r}_{1}$ | 90.5 | 90.8 | 90.4 | 543.4 |  |
|  | $\mathrm{r}_{2}$ | 90.7 | 90.9 | 90.1 |  |  |
|  |  | 542.2 | 544.1 | 541.1 | 1627.4 |  |

(3) alpha=0.05

Solution//
Let Temperature $=$ Factor $A$ then ( $a 1=150, a 2=160, a 3=170$ ) Let Pressure= Factor B then ( $b 1=200, b 2=215, b 3=230$ ), alpha=5\%
$1=3-1=2$
d. $f_{1 B}=a-1=3-1=2$
d.f. ${ }_{1 A B}=(a-1)(b-1)=(3-1)(3-1)=2 * 2=4$

(1) $\quad \mathrm{H}_{\mathrm{OA}}: \mu_{1}=\mu_{2}=\mu_{3}$
$\mathrm{F}_{\mathrm{A}(0.05,2,9)=} 4.2565$
$\mathrm{H}_{0 \mathrm{~B}}: \mu_{1}=\mu_{2}=\mu_{3} \quad \mathrm{~F}_{\mathrm{B}(0.05,2,9)=4.2565}$
$\mathrm{H}_{0 \mathrm{AB}}: \mu_{11}=\mu_{12}=\cdots=\mu_{33}$
$\mathrm{F}_{\mathrm{AB}(0.05,4,9)=} \mathbf{3 . 6 3 3 1}$
$\mathrm{F}_{(0.05 ; 3 ; 6)}=4.7571$
$\mathrm{F}_{(0.05 ; 6 ; 3)}=8.9407$
$\mathrm{F}_{(0.05 ; 2,9)}=4.2565$
$\mathrm{F}_{(0.05 ; 4,9)}=3.6331$

$$
\text { d.f. } 2=\text { d.f. } \text { Error }=a b(r-1)=3^{*} 3^{*}(2-1)=9
$$

$\mathrm{H}_{1 \mathrm{~A}}$ : at least two means are not equal
$H_{1 B}$ : at least two means are not equal
$\mathrm{H}_{1 \mathrm{AB}}$ at least two means are not equal

(4)
$Y . . .=1627.4$
$C . F .=\frac{(Y \ldots)^{2}}{a b r}=\frac{(1627.4)^{2}}{3(3)(2)}=147135.04$


$$
\begin{aligned}
& \mathrm{SSAB}=\frac{\sum_{i=1}^{3} \sum_{j=1}^{3} Y_{i j .}^{2}}{r}-C . F .-S S A-S S B \\
&=\frac{180.6^{2}+180.4^{2}+\cdots+180.5^{2}}{2}-147135.04-0.301-0.786= \\
&=147135.81-147135.04 \\
&=0.069
\end{aligned}
$$

$\mathrm{SST}=\sum_{i=1}^{3} \sum_{j=1}^{3} \sum_{k=1}^{2}\left(Y_{i j k}^{2}\right)-C . F .=\left(90.4^{2}+90.2^{2}+\ldots+90.1^{2}\right)-147135.04$
$\mathrm{SSA}=\frac{\sum_{i=1}^{3} Y_{i .}^{2}}{b r}-C . F .=\frac{542.5^{2}+541.5^{2}+543.4^{2}}{3(2)}-147135.04$
$=147135.34-147135.04=0.301$

| S.O.V. | d.f. | S.S. | MS | F cal. | F $_{\text {tab. }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Factor A | 2 | 0.301 | 0.151 | $* 8.466$ | 4.256 |
| Factor B | 2 | 0.768 | 0.384 | $* 21.6$ | 4.256 |
| Interaction AB | 4 | 0.069 | 0.017 | 0.97 | 3.633 |
| Error | 9 | 0.16 | 0.018 |  |  |
| Total | 17 | 1.298 |  |  |  |

(5) We reject $\mathrm{H}_{0 A}$ and $\mathrm{H}_{0 B}$ only.

Q2// A) From the ANOVA table below (LSD Latin Square Design) find the relative efficiency of RE (LSD: $\operatorname{RCBD}_{\text {(Row \& Columns) }}$ and RE (LSD: CRD):

| S.O.V. | d.f. | SS | MS |
| :---: | :---: | :---: | :---: |
| Row | 4 | 5.6 |  |
| Column | 4 | 63.2 |  |
| treatments | 4 | 46.3 |  |
| Error | 12 | 3.54 |  |

$$
\begin{aligned}
& \text { R.E. }_{(\text {(D.RCCBD } \text { Row })}=\frac{M S_{C o l .}+(r-1) M S_{E}}{r M S_{E}} \times 100 \\
& \text { RE. }_{(\text {LD.CRD) }}=\frac{M S_{\text {Row }}+M S_{\text {Col }}+(r-1) M S_{E}}{(r+1) M S_{E}} \times 100
\end{aligned}
$$

1) $1151.186 \%$ (RE for LSD better than RCBD Row.)
2) $174.9153 \% \quad$ (RE for LSD better than RCBD ${ }_{\text {Col. }}$ )
3) $1038.418 \%$ (RE for LSD better than CRD)

Q2// B) Use LSD $\alpha$ with five stapeses, for the following information at alpha= 0.05 :
(10 Marks)

| t 1 | t 2 | t 3 | t 4 | t 5 |
| :---: | :---: | :---: | :---: | :---: |
| 4 | 12 | 6 | 20 | 2 |
| 5 | 14 | 8 | 21 | 3 |
| 2 | 13 | 7 | 26 |  |
| 3 |  |  | 28 |  |


| S.O.V. | SS | df | MS | Fcal. | Ftab. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| treatments | 1079.5 | 4 | 269.875 | 54.721 | 3.35669 | $t_{(0.025 ; 11)}=2.201$ |
| Error | 54.25 | 11 | 4.932 |  |  |  |
| Total | 1133.75 | 15 |  |  |  |  |

Solution: Let Alpha =0.05

(1) $H_{0}: \mu_{1}=\mu_{2}, \mu_{1}=\mu_{3}, \ldots, \mu_{4}=\mu_{5}$
(2) $H_{1}: \mu_{1} \neq \mu_{2}, \mu_{1} \neq \mu_{3}, \ldots, \mu_{4} \neq \mu_{5}$

$$
\begin{aligned}
& \text { (3) } \alpha=0.05 \rightarrow \frac{\alpha}{2}=0.025 \\
& \text { def. } \text { Error }=11 \text { then : } \\
& \left.t_{\left(\frac{\tilde{\sigma}}{2}\right.} \text { d.f.Error }\right)=t_{(0.025 ; 11)}=2.201 \\
& L S D_{\alpha\left(\mu_{1}=\mu_{2}, \mu_{1}=\mu_{3}, \mu_{2}=\mu_{4}, \mu_{3}=\mu_{4}\right)}=t_{\left(\frac{\tilde{\sigma}}{2} d . f E r r o r\right)} \times \sqrt{M S E\left(\frac{1}{r_{1}}+\frac{1}{r_{2}}\right)}=t_{((0.025,11)} \times \sqrt{M S E\left(\frac{1}{4}+\frac{1}{3}\right)} \\
& =t_{(0.025,11)} \times \sqrt{\operatorname{MSE}\left(\frac{1}{4}+\frac{1}{3}\right)}=2.201 \times \sqrt{4.932\left(\frac{1}{4}+\frac{1}{3}\right)}=3.733 \\
& L S D_{\alpha\left(\mu_{1}=\mu_{4}\right)}=t_{(0.025 ; 11)} \times \sqrt{M S E\left(\frac{1}{4}+\frac{1}{4}\right)}=2.201 \times \sqrt{4.932\left(\frac{1}{4}+\frac{1}{4}\right)}=3.456 \\
& L S D_{\alpha\left(\mu_{1}=\mu_{5 S} \mu_{4}=\mu_{5}\right)}=t_{(0.025: 11)} \times \sqrt{M S E\left(\frac{1}{4}+\frac{1}{2}\right)}=2.201 \times \sqrt{4.932\left(\frac{1}{4}+\frac{1}{2}\right)}=4.233 \\
& L S D_{\alpha\left(\mu_{2}=\mu_{3}\right)}=t_{(0.025 ; 11)} \times \sqrt{M S E\left(\frac{1}{3}+\frac{1}{3}\right)}=2.201 \times \sqrt{4.932\left(\frac{1}{3}+\frac{1}{3}\right)}=3.991 \\
& L S D_{\alpha\left(\mu_{2}=\mu_{S}, \mu_{3}=\mu_{5}\right)}=t_{(0.025 ; 11)} \times \sqrt{M S E\left(\frac{1}{3}+\frac{1}{2}\right)}=2.201 \times \sqrt{4.932\left(\frac{1}{3}+\frac{1}{2}\right)}=4.462
\end{aligned}
$$



(5) we not reject $H_{0}: \mu_{1}=\mu_{3}, \mu_{1}=\mu_{5}$ only.

Salahaddin University-Erbil
College of Administration and Economics


Subject: Experimental Design
Date: 26-5-2021 Wednesday
Stage: four
Time: 2 Hours

Q1//
A) Create the design for:
(15 Marks)
3- CRD with four replications and four treatments.
4- CRD ( $\mathrm{S}=4, \mathrm{t}=3, \mathrm{r}=2$ ).
5- RCBD with four Blocks and four treatments after that if we have messing data in $\mathrm{Y}_{32}$.
6- GLS (Graeco Latin Square Design) with six replications.
7- Factorial CRD $(2 \times 3 \times 2)$ with two replications.
B) Create the Linear Model for:
3. $\operatorname{RCBD}(t=4, r=5)$
4. Sampling CRD if $(t=5, r=4, s=6)$.
5. LSD (Latin Square Design) if $\mathrm{r}=8$.
6. GLS (Graeco Latin Square Design) with seven replications.
7. Factorial CRD $(8 \times 5 \times 4)$ with ten replications.

Q2// A) from the following data (Latin Square Design) test if there are any deferent or not? If alpha=0.05:
(15 Marks)

| Row | Column 1 | Column 2 | Column 3 | Column 4 | Rows Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $1(\mathrm{~A})$ | $2(\mathrm{C})$ | $4(\mathrm{~B})$ | $2(\mathrm{D})$ | 9 |
| 2 | $2(\mathrm{C})$ | $2(\mathrm{~A})$ | $1(\mathrm{D})$ | $6(\mathrm{~B})$ | 11 |
| 3 | $5(\mathrm{~B})$ | 1(D) | $0(\mathrm{~A})$ | $2(\mathrm{C})$ | 8 |
| 4 | 1 (D) | 9(B) | $2(\mathrm{C})$ | $1(\mathrm{~A})$ | 13 |
| Columns Total | 9 | 14 | 7 | 11 | 41 |

B) From (Q2// A) above find $\operatorname{LSD}_{a}$ (Least Significant Difference) with 5 stapes. (10 Marks)

Q3// From the ANOVA table below (LSD Latin Square Design) find the relative efficiency of RE (LSD: $\operatorname{RCBD}_{\text {(Row \& columns) }}$ and RE (LSD: CRD):
(10 Marks)

| S.O.V. | d.f. | SS | MS |
| :---: | :---: | :---: | :---: |
| Row | 4 | 1.34 |  |
| Column | 4 | 2.83 |  |
| treatments | 4 | 3.44 |  |
| Error | 12 | 0.12 |  |

if $\mathrm{F}_{(0.05 ; 3 ; 6)}=4.7571, \mathrm{~F}_{(0.05 ; 6 ; 3)}=8.9407, \mathrm{~F}_{(0.01 ; 3 ; 6)}=9.7795, \mathrm{~F}_{(0.01 ; 6 ; 3)}=27.9107, \mathrm{t}_{(0.025,6)}=2.496$,
$R . E_{\left(L D D R C B D_{\text {Row }}\right)}=\frac{M S_{C o l .}+(r-1) M S_{E}}{r M S_{E}} \times 100 \quad$ R.E. . $\left.L D . C R D\right)=\frac{M S_{\text {Row }}+M S_{C o l}+(r-1) M S_{E}}{(r+1) M S_{E}} \times 100$

## Good Luck



Dr. Omiad Saber Abdullah Shwany

Salahaddin University-Erbil
College of Administration and Economics
Department: Statistics and Information
Final Exam: $2^{\text {nd }}$ Trial 2020-2021

Subject: Experimental Design
Date: -6-2021
Stage: four
Time: 2 Hours

Q1//
A) Create the design for:
(15 Marks)
8- CRD ( $\mathrm{S}=6, \mathrm{t}=3, \mathrm{r}=2$ ).
9- Factorial CRD $(2 \times 2 \times 2)$ with two replications.
$10-\mathrm{CRD}$ with three replications and three treatments.
11- GLS (Graeco Latin Square Design) with four replications.
12- RCBD with three Blocks and four treatments after that if we have messing data in $\mathrm{Y}_{42}$.
B) Create the Linear Model for:
(10 Marks)
8. GLS (Graeco Latin Square Design) with 10 replications.
9. Factorial CRD $(5 \times 6 \times 7)$ with ten replications.
10. LSD (Latin Square Design) if $\mathrm{r}=7$.
11. Sampling CRD if $(t=6, r=4, s=8)$.
12. $\operatorname{RCBD}(\mathrm{t}=6, \mathrm{r}=4)$

Q2// A) from the following data (CRD) test if there are any deferent or not? If alpha=0.05:
(15 Marks)

| Replicate | Treatment |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | t 1 | t 2 | t 3 | t 4 |
| 1 | 2 | 1.7 | 2 | 2.1 |
| 2 | 2.2 | 1.9 | 2.4 | 2.2 |
| 3 | 1.8 | 1.5 | 2.7 | 2.2 |
| 4 | 2.3 |  | 2.5 | 1.9 |
| 5 | 1.7 |  | 2.4 |  |

B) From (Q2// A) above find $\mathrm{LSD}_{a}$ (Least Significant Difference) with 5 stapeses. (10 Marks)

Q3// From the ANOVA table below (LSD Latin Square Design) find the relative efficiency of RE (LSD: RCBD (Row \& Columns) and RE (LSD: CRD):
(10 Marks)

| S.O.V. | d.f. | SS | MS |
| :---: | :---: | :---: | :---: |
| Row | 4 | 0.05 |  |
| Column | 4 | 0.72 |  |
| treatments | 4 | 2.65 |  |
| Error | 12 | 0.12 |  |

if $\mathrm{F}_{(0.025 ; 3 ; 13)}=4.3472, \mathrm{~F}_{(0.05 ; 3 ; 13)}=3.4105, \mathrm{~F}_{(0.01 ; 3 ; 13)}=5.7394, \mathrm{~F}_{(0.05 ; 13 ; 3)}=26.9831, \mathrm{t}_{(0.025,13)}=2.16$,
R.E. $._{(L D . C R D)}=\frac{M S_{\text {Row }}+M S_{\text {Col }}+(r-1) M S_{E}}{(r+1) M S_{E}} \times 100 \quad$ R.E. $_{\left(L D D R C B D_{\text {Row }}\right)}=\frac{M S_{\text {Col }}+(r-1) M S_{E}}{r M S_{E}} \times 100$

## Good Luck



Dr. Omiad Saber Abdullah Shwany

Salahaddin University-Erbil
College of Administration and Economics


Subject: Experimental Design
Date: 26-5-2021 Wednesday
Stage: four
Time: 2 Hours

Q1//
A) Create the design for:
(15 Marks)
13-CRD with four replications and four treatments.
14- CRD ( $\mathrm{S}=4, \mathrm{t}=3, \mathrm{r}=2$ ).
15- RCBD with four Blocks and four treatments after that if we have messing data in $\mathrm{Y}_{32}$.
16- GLS (Graeco Latin Square Design) with six replications.
17 - Factorial CRD $(2 \times 3 \times 2)$ with two replications.
B) Create the Linear Model for:
13. $\operatorname{RCBD}(\mathrm{t}=4, \mathrm{r}=5)$
14. Sampling CRD if $(t=5, r=4, s=6)$.
15. LSD (Latin Square Design) if $\mathrm{r}=8$.
16. GLS (Graeco Latin Square Design) with seven replications.
17. Factorial CRD $(8 \times 5 \times 4)$ with ten replications.

Q2// A) from the following data (Latin Square Design) test if there are any deferent or not? If alpha=0.05:
(15 Marks)

| Row | Column 1 | Column 2 | Column 3 | Column 4 | Rows Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $1(\mathrm{~A})$ | $2(\mathrm{C})$ | $4(\mathrm{~B})$ | $2(\mathrm{D})$ | 9 |
| 2 | $2(\mathrm{C})$ | $2(\mathrm{~A})$ | $1(\mathrm{D})$ | $6(\mathrm{~B})$ | 11 |
| 3 | $5(\mathrm{~B})$ | 1(D) | $0(\mathrm{~A})$ | $2(\mathrm{C})$ | 8 |
| 4 | 1 (D) | 9(B) | $2(\mathrm{C})$ | $1(\mathrm{~A})$ | 13 |
| Columns Total | 9 | 14 | 7 | 11 | 41 |

B) From (Q2// A) above find $\operatorname{LSD}_{a}$ (Least Significant Difference) with 5 stapes. (10 Marks)

Q3// From the ANOVA table below (LSD Latin Square Design) find the relative efficiency of RE (LSD: $\operatorname{RCBD}_{\text {(Row \& Columns) }}$ and RE (LSD: CRD):
(10 Marks)

| S.O.V. | d.f. | SS | MS |
| :---: | :---: | :---: | :---: |
| Row | 4 | 1.34 |  |
| Column | 4 | 2.83 |  |
| treatments | 4 | 3.44 |  |
| Error | 12 | 0.12 |  |

if $\mathrm{F}_{(0.05 ; 3 ; 6)}=4.7571, \mathrm{~F}_{(0.05 ; 6 ; 3)}=8.9407, \mathrm{~F}_{(0.01 ; 3 ; 6)}=9.7795, \mathrm{~F}_{(0.01 ; 6 ; 3)}=27.9107, \mathrm{t}_{(0.025,6)}=2.496$,
$R . E_{\left(L D D R C B D_{\text {Row }}\right)}=\frac{M S_{C o l .}+(r-1) M S_{E}}{r M S_{E}} \times 100 \quad$ R.E. . $\left.L D . C R D\right)=\frac{M S_{\text {Row }}+M S_{C o l}+(r-1) M S_{E}}{(r+1) M S_{E}} \times 100$

## Good Luck



Dr. Omiad Saber Abdullah Shwany

Experimental Design and Analysis
Time: 90 minutes
$2^{\text {nd }}$ Examination
Date: 8-5-2014 Thursday

University of Salahadden-Erbil Collage of Adm. and Economics
Statistics Department $4^{\text {th }}$ Stage

Q1// Create the design (انشاء تصميم) and find the Linear Model for:
1- ( $4 \times 2$ ) CRD with 3 replications.
2- $(3 \times 3)$ RCBD with 2 Blocks.
3- $2^{3}$ confounding 2 blocks and 3repleaction.
4- RCBD $(4 \times 3) r=3$ if Factor A is Whole Plots and Factor B (Sub-plot).

Q2// Define these designs (ما نوع النصميم المستخدم) and find the linear model: (20 Degrees)
(A)

|  | c1 |  | c2 |  | c3 |  | c4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| r1 | b1 | a4 | b1 | a2 | b3 | a3 | b2 | al |
|  | b3 |  | b2 |  | b2 |  | b3 |  |
|  | b2 |  | b3 |  | b1 |  | b1 |  |
| r2 | b3 | a3 | b2 | al | b3 | a2 | b3 | a4 |
|  | b2 |  | b3 |  | b1 |  | b1 |  |
|  | b1 |  | b1 |  | b2 |  | b2 |  |
| r3 | b3 | a1 | b2 | a3 | b1 | a4 | b3 | a2 |
|  | b2 |  | b1 |  | b2 |  | b2 |  |
|  | b1 |  | b3 |  | b3 |  | b1 |  |
| r4 | b2 | a2 | b1 | a4 | b1 | al | b2 | a3 |
|  | b1 |  | b3 |  | b3 |  | b1 |  |
|  | b3 |  | b2 |  | b2 |  | b3 |  |

(B)


Q3// Test the hypotheses with LSD if possible for:
(40 Degrees)

| Row | Column 1 | Column 2 | Column 3 | Column 4 | Row $\left(\sum R\right)$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 1 | $1.640(\mathrm{~B})$ | $1.210(\mathrm{D})$ | $1.425(\mathrm{C})$ | $1.345(\mathrm{~A})$ | 5.620 |
| 2 | $1.475(\mathrm{C})$ | $1.185(\mathrm{~A})$ | $1.400(\mathrm{D})$ | $1.290(\mathrm{~B})$ | 5.350 |
| 3 | $1.670(\mathrm{~A})$ | $0.710(\mathrm{C})$ | $1.665(\mathrm{~B})$ | $1.180(\mathrm{D})$ | 5.225 |
| 4 | $1.565(\mathrm{D})$ | $1.290(\mathrm{~B})$ | $1.655(\mathrm{~A})$ | $0.660(\mathrm{C})$ | 5.170 |
| Column total $\left(\sum C\right)$ | 6.350 | 4.395 | 6.145 | 4.475 | 21.365 |

If $\Longleftrightarrow F_{(0.05 ; 3 ; 3)}=9.2766, F_{(0.025 ; 3 ; 6)}=15.439, \mathrm{t}_{(0.05 ; 6)}=2.4469 ; \mathrm{t}_{(0.025 ; 6)}=2.9687 ; \mathrm{F}_{(0.05 ; 3 ; 6)}=4.7571$

| Treatment | Total |
| :---: | :---: |
| A | 5.855 |
| B | 5.885 |
| C | 4.270 |
| D | 5.355 |

Experimental Design and Analysis
Time: 90 minutes
$3^{\text {rd }}$ Examination
Date: 18-5-2014 Sunday

Q1// Create the design (انشاء تصميم) and find the Linear Model for:
1- $2^{3}$ confounding 2 blocks and 2 replications.
2- GLS with 4 treatments.
3- ( $2 \times 4$ ) RCBD with 3 Blocks.
4- RCBD $(4 \times 3) \mathrm{r}=4$ if Factor A is Whole Plots and Factor B (Sub-plot).
5- ( $2 \times 5$ ) CRD with 3 replications.

Q2// The yield (نتيجه) of a chemical process is being studied. The two most important variables are thought to be the pressure and the temperature. Three levels of each factor are selected, and a factorial experiment with two replicates is performed. The yield data follow; Test the hypotheses with LSD if possible:
Degrees)

| Temperature | Replications | Pressure |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 200 | 215 | 230 | Sum Rows |
| 150 | $r_{1}$ | 90.4 | 90.7 | 90.2 | 542.5 |
|  | $r_{2}$ | 90.2 | 90.6 | 90.4 |  |
| 160 | $r_{1}$ | 90.1 | 90.5 | 89.9 | 541.5 |
|  | $r_{2}$ | 90.3 | 90.6 | 90.1 |  |
| 170 | $r_{1}$ | 90.5 | 90.8 | 90.4 | 543.4 |
|  | $r_{2}$ | 90.7 | 90.9 | 90.1 |  |
| Sum Columns |  | 542.2 | 544.1 | 541.1 | 1627.4 |

If $\Longleftrightarrow \mathrm{F}_{(0.01 ; 2 ; 2)}=99, \mathrm{~F}_{(0.025 ; 2 ; 9)}=5.7147, \mathrm{~F}_{(0.05 ; 2 ; 9)}=4.2565, \mathrm{t}_{(0.025 ; 9)}=2.685 ; \mathrm{t}_{(0.05 ; 9)}=2.262$

Experimental Design and Analysis
Time: 90 minutes
$1^{s t}$ Examination

University of Salahadden-Erbil
Collage of Administration and Economics
Statistics Department $4^{\text {th }}$ Stage

Q1// create the design and find the Linear Model for (ديز اين و موّديّل بدوّزموه):
1- CRD with four replications and five treatments if $t_{3}$ is missing.
2- RCBD with three Blocks and four treatments.
Q2// from the following information (CRD design) do the Duncan multiple range test with five stapes if MSE=6.23 and alpha=5\%:
Degrees)

| Treatments | $\mathrm{t}_{1}$ | $\mathrm{t}_{2}$ | $\mathrm{t}_{3}$ | $\mathrm{t}_{4}$ | $\mathrm{t}_{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Mean Value | 6.4 | 8.7 | 9.1 | 16.3 | 14 |
| r | 4 | 6 | 8 | 7 | 5 |

Q3// find ANOVA with 5 stapes:
(30 Degrees)

| Blocks | Treatment |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{t}_{1}$ | $\mathrm{t}_{2}$ | $\mathrm{t}_{3}$ | $\mathrm{t}_{4}$ |
| 1 | 9 | 11 | 4 | 7 |
| 2 | 8 | 13 | 6 | 10 |
| 3 | 9 | 8 | 7 | 5 |

if : $\mathrm{F}_{(0.01 ; 6,3)}=27.9107, \mathrm{~F}_{(0.01 ; 3,6)}=9.7795, \mathrm{~F}_{(0.05 ; 3,6)}=4.7571, \mathrm{~F}_{(0.05 ; 6,3)}=8.9406$

Critical values $\mathrm{q}^{\prime}(\mathrm{p}, \mathrm{df} ; 0.05)$ for Duncan's multiple range tests

| d.f.Error | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 3.635 | 3.749 | 3.796 | 3.814 | 3.814 | 3.814 | 3.814 | 3.814 |
| $:$ | $:$ | $:$ | $:$ | $:$ | $:$ | $:$ | $:$ | $:$ |
| 25 | 2.913 | 3.059 | 3.154 | 3.221 | 3.271 | 3.310 | 3.341 | 3.366 |
| 29 | 2.892 | 3.039 | 3.135 | 3.202 | 3.253 | 3.293 | 3.326 | 3.352 |
| 30 | 2.888 | 3.035 | 3.131 | 3.199 | 3.250 | 3.290 | 3.322 | 3.349 |

Experimental Design and Analysis
Time: 90 minutes
Date: 6-2-2019 Thursday

University of Salahadden-Erbil
Collage of Administration and Economics
Statistics Department $4^{\text {th }}$ Stage

Q1// create the design and find the Linear Model for:
1- CRD with three replications and five treatments.
2- CRD with two replications and four treatments and 5 samples.
Q2// from the following information (CRD design) do the Duncan multiple range test with five stapeses if MSE=8.23 and alpha=5\%:
(35 Degrees)

| Treatments | $\mathrm{t}_{1}$ | $\mathrm{t}_{2}$ | $\mathrm{t}_{3}$ | $\mathrm{t}_{4}$ | $\mathrm{t}_{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Mean Value | 4.31 | 8.7 | 19.1 | 16.3 | 14 |
| r | 4 | 6 | 8 | 7 | 5 |

Q3// find ANOVA with 5 stapes if alpha 2.5\%:

| replications | Treatment |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{t}_{1}$ | $\mathrm{t}_{2}$ | $\mathrm{t}_{3}$ | $\mathrm{t}_{4}$ |
| 1 | 9 | 11 | 4 | 7 |
| 2 | 8 | 13 | 6 | 10 |
| 3 | 9 | 8 | 7 | 5 |
| 4 | 10 | 15 | 8 | 8 |

if: $\mathrm{F}_{(0.05 ; 3,12)}=3.4903, \mathrm{~F}_{(0.05 ; 12,3)}=8.7446, \mathrm{~F}_{(0.025 ; 3,12)}=4.4742, \mathrm{~F}_{(0.025 ; 12,3)}=14.3366$

Critical values $\mathrm{q}^{\prime}(\mathrm{p}, \mathrm{df} ; 0.05)$ for Duncan's multiple range tests

| d.f.Error | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | 3.635 | 3.749 | 3.796 | 3.814 | 3.814 | 3.814 | 3.814 | 3.814 |
| $:$ | $:$ | $:$ | $:$ | $:$ | $:$ | $:$ | $:$ | $:$ |
| 25 | 2.913 | 3.059 | 3.154 | 3.221 | 3.271 | 3.310 | 3.341 | 3.366 |
| 29 | 2.892 | 3.039 | 3.135 | 3.202 | 3.253 | 3.293 | 3.326 | 3.352 |
| 30 | 2.888 | 3.035 | 3.131 | 3.199 | 3.250 | 3.290 | 3.322 | 3.349 |

Q1// Create the design and find the Linear Model for:
1- $(2 \times 3 \times 2)$ CRD with 3 replications.
2- LSD (Latin Square Design) with 5 treatments.
3- GLS (Graeco-Latin Square Design) with 4 treatments.
4- $(4 \times 3)$ CRD with 2 replications.
5- RCBD (4 treatments, 2 Blocks)

Q2// Test the hypotheses of this design (Factorial CRD):

| Temperature | Replications | Pressure |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{b}_{1}$ | $\mathrm{~b}_{2}$ | $\mathrm{~b}_{3}$ |
| $\mathrm{a}_{1}$ | $\mathrm{r}_{1}$ | 4 | 7 | 2 |
|  | $\mathrm{r}_{2}$ | 2 | 6 | 4 |
| $\mathrm{a}_{2}$ | $\mathrm{r}_{1}$ | 1 | 5 | -1 |
|  | $\mathrm{r}_{2}$ | 3 | 6 | 1 |
| $\mathrm{a}_{3}$ | $\mathrm{r}_{1}$ | 5 | 8 | 4 |
|  | $\mathrm{r}_{2}$ | 7 | 9 | 1 |

If :

$$
\begin{aligned}
& F_{(0.01,2,9)}=8.0215, F_{(0.01,9,2)}=99.3881, F_{(0.01,4,9)}=6.4221, F_{(0.01,9,4)}=14.6591 \\
& F_{(0.05,2,9)}=4.2565, F_{(0.05,9,2)}=19.3848, F_{(0.05,4,9)}=3.6331, F_{(0.05,9,4)}=5.9988
\end{aligned}
$$



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## Final Exam - Second Semester - $1^{\text {st }}$ trail 2022-2023

Q1-A// Create the design for:
1- $\quad$ CRD $(3 \times 4) r=2$
2- RCBD with 2 Blocks and 5 treatments
3- LSD ( $\mathrm{t}=4$ ) after that if we have messing data in $\mathrm{Y}_{342}$
4- GLSD if $(\mathrm{t}=5)$
Q1-B// Find the linear model for:
( $4 \times 3=12$ Marks)

1- GLSD ( $\mathrm{t}=11$ )
2- LSD ( $\mathrm{t}=9$ )
3- CRD ( $\mathrm{S}=8, \mathrm{t}=7, \mathrm{r}=3$ )
4- CRD ( $6 \times 8$ ) r=12

Q2// from the following Data, do the five stapes to know if there are differences or not between treatments?

$$
\text { ( } 5 \times 4=20 \text { Marks) }
$$

| $\mathrm{B} \beta(3)$ | $\mathrm{C} \gamma(2)$ | $\mathrm{A} \alpha(9)$ | $\mathrm{D} \delta(1)$ | $\mathrm{F}_{(0.05,3,15)}=3.2874$ |
| :---: | :---: | :---: | :---: | :--- |
| $\mathrm{D} \alpha(2)$ | $\mathrm{A} \delta(10)$ | $\mathrm{C} \beta(3)$ | $\mathrm{B} \gamma(4)$ | $\mathrm{F}_{(0,0.1,2,3)}=27.052$ |
| $\mathrm{~A} \gamma(11)$ | $\mathrm{D} \beta(2)$ | $\mathrm{B} \delta(2)$ | $\mathrm{C} \alpha(3)$ | $\mathrm{F}_{(0,053,3,3}=9.2766$ |
| $\mathrm{C} \delta(3)$ | $\mathrm{B} \alpha(2)$ | $\mathrm{D} \gamma(2)$ | $\mathrm{A} \beta(10)$ | $\mathrm{F}_{(0.01,3,3)}=29.4567$ |

Q3_A// Prove that TSS $=\mathrm{SSt}+\mathrm{SSE}$ in CRD.

Q3_B// From the ANOVA table for (RCBD) design compare between the relative efficiency of (RCBD) and (CRD) design:
(8 Marks)

| S.O.V. | d.f. | S.S. |
| :---: | :---: | :---: |
| Block | 4 | 4.23 |
| Treatment | 3 | 13.2 |
| Error | 12 | 26.26 |
| Total | 19 |  |

Good Luck

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Higher Edu. and Sci. Research Ministry
Salahaddin University
College of Administration \& Economic Statistics and Informatics Department


Subject: Testing Hypothesis
Stage: $4^{\text {th }}$ Class
Time: 2 Hours
Date: / /2022

## Final Exam - First Semester 2022-2023

Q1// The following information is related to the rubber percentage of two types of Rubber plants, where the sample have been drawn independently. Test for their mean difference at the 5\% significant level. Assume that the population variances are not known and are unequal.

15 Marks

|  | Type I | Type II |
| :---: | :---: | :---: |
| n | 12 | 12 |
| Mean | 5.63 | 6.74 |
| Variance | 0.38 | 1.45 |



Q2// Let's we have 5 treatment groups $t_{1}, t_{2}, t_{3}, t_{4}$, and $t_{5}$. Test for their mean difference at the $5 \%$ significant level and $(\mathrm{MSE}=5.2)$. Find the Least Significant Difference (LSD $\alpha$ ).

15 Marks

| $\mathbf{t}_{\mathbf{1}}$ | $\mathbf{t}_{\mathbf{2}}$ | $\mathbf{t}_{\mathbf{3}}$ | $\mathbf{t}_{\mathbf{4}}$ | $\mathbf{t}_{\mathbf{5}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 4 | 10 | 28 | 3 | 8 |
| 5 | 14 | 21 | 4 | 9 |
| 2 | 11 | 24 |  | 6 |
| 3 |  | 20 |  |  |

Q3// If have a random sample of 500 American adults who are questioned regarding their political affiliation and opinion on a tax reform bill. We will test if the political affiliation and their opinion on a tax reform bill are dependent at a 5\% level of significance. Calculate the Chi-Square Test of Independence.



## 15 Marks

|  | Favor | Indifferent | Opposed |
| :---: | :---: | :---: | :---: |
| Democrat | 138 | 83 | 64 |
| Republican | 64 | 67 | 84 |

Q4// Answer 5 only:

1. What are the Type I Error and Type II Error?
2. Describe Critical region, Critical Value by chart.
3. Describe one tail and two tail tests?
4. What are the Hypothese for One Sample $t$-test?
5. What are the differences between Statistic and Parameter?

6 . What are the differences between Z -test and t -test?

If we have the following tabulated value:

| $\mathrm{t}_{(0.025 ; 23)}=2.069$ | $\mathrm{t}_{(0.025 ; 22)}=2.074$ | $\mathrm{t}_{(0.05 ; 22)}=1.717$ | $\mathrm{Z}_{(0.025)}=1.96$ | $\mathrm{Z}_{(0.05)}=1.645$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~F}_{(0.05 ; 5,11)}=3.2039$ | $\mathrm{~F}_{(0.05 ; 4,11)}=3.3567$ | $\mathrm{~F}_{(0.025 ; 4,16)}=3.0069$ | $x^{2}{ }_{(0.05 ; 6)}=12.59$ | $x^{2}{ }_{(0.05 ; 2)}=5.99$ |

## Good Luck

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Examiner

Dr. Omiad Saber Abdullah
Examiner

Higher Edu. and Sci. Research Ministry Salahaddin University-Erbil College of Administration \& Economic Statistics and Informatics Department


Subject: Testing Hypothesis
Stage: $4^{\text {th }}$ Class
Time: 2 Hours
Date: / 1 /2023

Final Exam - First Semester- $\mathbf{2}^{\text {nd }}$ Trial 2022-2023

Q1// We randomly select 15 calls from each call center and calculate the average call lengths. The two call centers seem to have different average call lengths. Is this difference statistically significant? Assume these two samples come from populations with unequal variances. Use level of significance (0.05). 15 Marks

|  | Sample size | mean (sec) | Standard deviation |
| :--- | :---: | :---: | :---: |
| Call Center A | 15 | 122 | 15 |
| Call Center B | 15 | 135 | 20 |

Q2// The illness caused by a virus in a city concerning some restaurant inspectors is not consistent with their evaluations of the cleanliness of restaurants. In order to investigate this possibility, the director has five restaurant inspectors to grade the cleanliness of three restaurants. Carry out two-way ANOVA at $5 \%$ level of significance, the results are shown below. 15 Marks

| Inspectors <br> (Treatments) | Restaurants (Blocks) |  |  |
| :---: | :---: | :---: | :---: |
|  | I | II | III |
| 1 | 21 | 5 | 34 |
| 2 | 15 | 7 | 36 |
| 3 | 20 | 15 | 27 |
| 4 | 22 | 19 | 20 |
| 5 | 26 | 14 | 35 |

Q3// The following table shows three different airlines' row variables and the number of delayed or on-time flights column variable from light stats.com. Does on-time performance depend on the airline? Calculate the Chi-Square Test of Independence at 5\% level of significance.

15 Marks

|  | Delayed تاخير دهبيّت | On-time له كاتّى خوّى |
| :---: | :---: | :---: |
| American | 112 | 843 |
| Southwest | 114 | 1416 |
| United | 61 | 896 |

Q3// If we have the following information test the Dunnett test.
If MSE $=2.6$ and $\alpha=0.05$

## 15 Marks

| Treatments | Control <br> $\mathbf{t}_{\mathbf{1}}$ | $\mathbf{t}_{\mathbf{2}}$ | $\mathbf{t}_{\mathbf{3}}$ | $\mathbf{t}_{\mathbf{4}}$ |
| :---: | :---: | :---: | :---: | :---: |
| Mean | 4 | 8.5 | 7 | 11.5 |
| $\mathbf{n}$ | 5 | 3 | 4 | 3 |

If we have the following tabulated value:

| $\mathrm{t}_{(0.025 ; 29)}=2.045$ | $\mathrm{t}_{(0.025 ; 28)}=2.048$ | $\mathrm{t}_{(0.05 ; 29)}=1.699$ | $\mathrm{Z}_{(0.025)}=1.96$ | $\mathrm{Z}_{(0.05)}=1.645$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{t}_{(0.05 ; 28)}=1.701$ | $\mathrm{t}_{(0.025 ; 10)}=2.228$ | $\mathrm{t}_{(0.025 ; 11)}=2.201$ | $F_{(0.025 ; 4,10)}=4.271$ | $F_{(0.025 ; 5,10)}=4.236$ |
| $\mathrm{~F}_{(0.05 ; 4,8)}=3.838$ | $\mathrm{~F}_{(0.05 ; 4,10)}=3.48$ | $\mathrm{~F}_{(0.05 ; 2,8)}=4.459$ | $x^{2}{ }_{(0.05 ; 6)}=12.59$ | $x^{2}{ }_{(0.05 ; 2)}=5.99$ |
| Dunnett's $\mathrm{t}_{(0.05 ; 11)}=2.72$ |  |  |  |  |
| Dunnett's $\mathrm{t}_{(0.05 ; 14)}=2.63$ |  |  |  |  |

## Good Luck



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