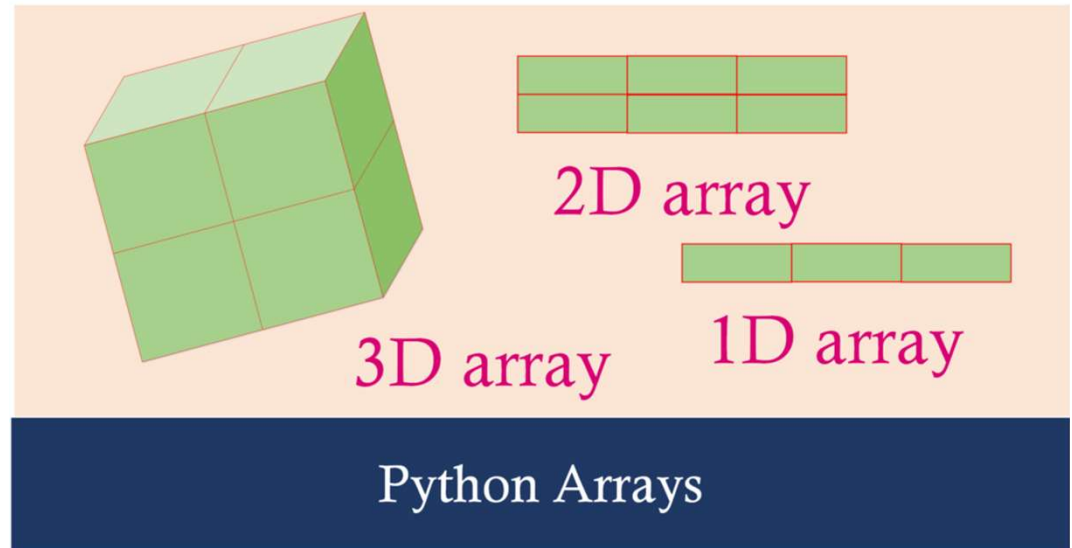


# Arrays

## Lecture 4: Arrays in python



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# Arrays in python

In many algorithms, data can be represented mathematically as a vector or a matrix.

The basic object in NumPy is the array

An array is a systematic arrangement of objects (usually numbers) in rows and columns or it is a list that contain mixed datatypes. An empty list can be utilized **by []** and **append** command can be used to merge data to the end of the list.

## 1-D Arrays

### Example

```
>>> import numpy as np

# Create a 1-D array by passing a list into NumPy's array() function.
>>> np.array([8, 4, 6, 0, 2])
array([8, 4, 6, 0, 2])

# The string representation has no commas or an array() label.
>>> x = np.array([1, 3, 5, 7, 9])
>>> print(x)
[1 3 5 7 9]
```

## 2-D Arrays

These are often used to represent matrix or 2nd order tensors.

```
import numpy as np

>>> x = np.array([[1, 2, 3], [4, 5, 6]])

>>> print(x)
[[1 2 3]
 [4 5 6]]
```

## 3-D arrays

Create a 3-D array with two 2-D arrays, both containing two arrays with the values 1,2,3 and 4,5,6:

```
import numpy as np

>>> x = np.array([[[1, 2, 3], [4, 5, 6]], [[1, 2, 3], [4, 5, 6]]])

>>> print(x)
[[[1 2 3]
  [4 5 6]]

 [[1 2 3]
  [4 5 6]]]
```

## Example

Check how many **dimensions** the arrays have:

```
import numpy as np

a = np.array(42)
b = np.array([1, 2, 3, 4, 5])
c = np.array([[1, 2, 3], [4, 5, 6]])
d = np.array([[[1, 2, 3], [4, 5, 6]], [[1, 2, 3], [4, 5, 6]]])

print(a.ndim)    0
print(b.ndim)    1
print(c.ndim)    2
print(d.ndim)    3
```

## list

### Example

```
>>>x = ["python", "programming"]
>>>x.append("physics")
>>>print x
['python', 'programming', 'physics']
```

Append a **single** element that will extend the list:

If you want to **extend** more than one **element** you should **use extend**, because you can only **append one element** or one **list** of element:

### Example

```
>>> x = [1,2]
>>>x.extend([3,4 5 ,6,7])
>>>print x
[1,2,3,4,5,6,7]
```

## ❑ An array can be defined by one of the four procedures

### 1) `arange`

The arguments of NumPy `arange()` that define the values contained in the array correspond to the numeric parameters start, stop, and step.

### 2) `ones`

This is an array where each and every element is one.

### 3) `zeros`

This array contains nothing but zeros.

### 4) `linspace`

NumPy `linspace` function returns an evenly spaced sequence of numbers for a given interval.

1) **Arange** works exactly the same as range, but produces an array instead of a list

### Example

```
>>> import numpy as np

>>> np.arange(10,0,-2)
>>> print x
[10 8 6 4 2]
```

Start = 10

Stop = 0

Step = -2

In this example, start is 10. Therefore, the first element of the obtained array is 10. step is -2, which is why your second value is 10-2, that is 8, while the third value in the array is 8-2, which equals 6.

```
>>> import numpy as np

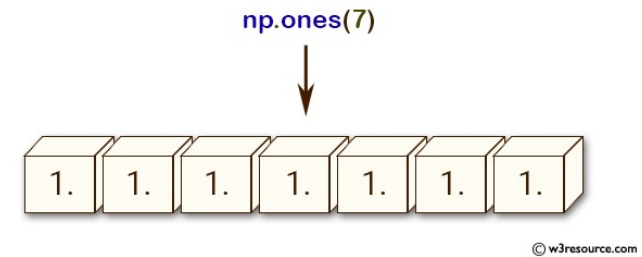
>>> np.arange(start=1, stop=10, step=3)
array([1, 4, 7])
```

**NOTE:** The value of **stop** is not included in an array.

2) **Ones** similarly creates an array of a certain size containing all ones.

Example

```
>>>x = ones(7)
>>>print x
[1. 1. 1. 1. 1. 1. 1.]
```



3) **The zeros()** function is used to get a new array of given shape and type, filled with zeros .

Example: numpy.zeros() function

```
>>> import numpy as np
```

Rows

Columns

```
>>> a = (3,2)
```

```
>>> np.zeros(a)
```

```
array([[ 0.,  0.],
       [ 0.,  0.],
       [ 0.,  0.]])
```

```
>>> x = zeros(4)
```

```
>>>print x
```

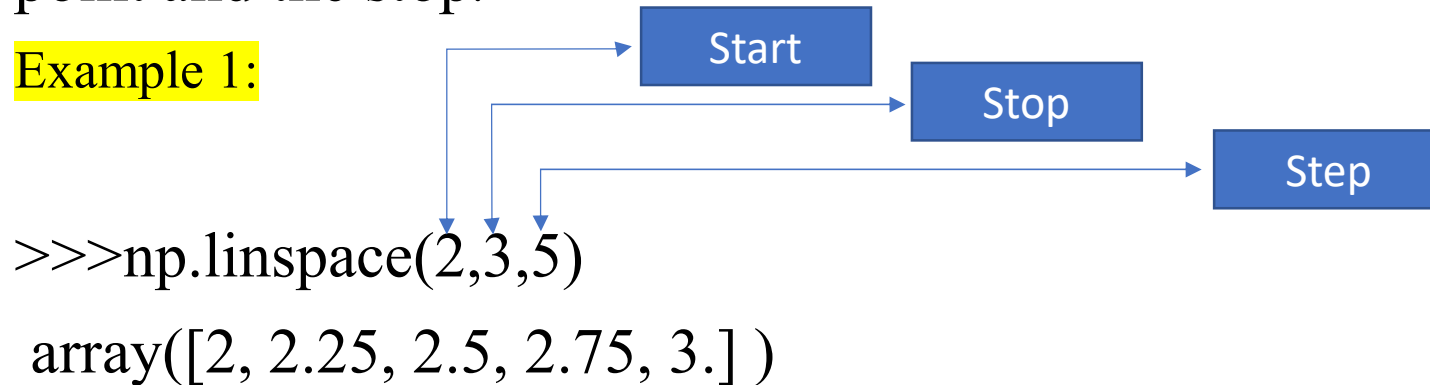
```
[0. 0. 0. 0.]
```



#### 4) **linspace**: linspace(start, stop, n=50)

Producing an array of n points evenly spaced between starting point and the stop.

**Example 1:**



**NOTE:** The value of **stop** is included in an array.

**Example 2:**

```
>>> np.linspace(2,3,5, endpoint=False)
array([2, 2.2, 2.4, 2.6, 2.8])
```

**Example 3:**

```
>>> np.linspace(2,3, 5, retstep=True)
(array([2,2.25,2.5,2.75,3],0.25)
```

**Note:** In general, we will select  $\text{start point} < \text{stop}$  so we can get an array where the entries are increasing in value. On the other hand, you can choose  $\text{start} = \text{stop}$  (to obtain an array with every value equal) or  $\text{start} > \text{stop}$  (to display an array with values decrease).

Example :

```
>>> np.linspace(2,10,4)
array([ 2.        ,  4.66666667,  7.33333333, 10.        ])
```

Example :

```
>>> np.linspace(2, 2, 5)
>>> array([2, 2, 2, 2, 2])
```

Example :

```
>>> np.linspace(3, 2, 5)
>>> array([3.  2.75  2.5  2.25  2])
```

An **arrays** in general are the main structure used in **NumPy**. Therefore all of the array **manipulations** and **creations techniques** that are **available** here are contained in the **NumPy package**.

**I= [a, b, c, d, ....]** defines **list, I, of numbers.**

**x= array([a, b, c, d,....])** defines an **array, x**

To produce an array of **float** numbers just we need to add **float** to the end.

**x= array([a, b, c, d, ....], dtype=float)**

**Example 1:**

```
>>> x=array([1,2,3,4,5])
```

```
>>> print x
```

```
[1 2 3 4 5]
```

**Example 2:**

```
>>> x= array ([1, 2, 3, 4, 5], dtype = float)
```

```
>>> print x
```

```
[1. 2. 3. 4. 5.]
```

# Operations with array

The calculation technique that we introduced in the last week can be applied on array as well. Every week we will be understanding an **extra methods** of **manipulating** and **calculating** with **arrays** so it is important to be **compatible** with the basic **ideas**. For now, we will just regard an array as a list of numbers. **Afterward**, we will see how the methods we introduce here can be applied to **vector calculations**, making **graphs**, and analysing our experimental data.

Lets start with these two arrays

```
>>> x= array([2, 1, 3, 5, 4], dtype= float)
```

```
>>> y= array([3, 1, 6, 2, 7], dtype= float)
```

## **1-Addition and subtraction of a constant.**

```
>>> z =x+5
```

```
>>>print z
```

```
[7. 6. 8. 10. 9. ]
```

```
>>> z= y-2
```

```
>>>print z
```

```
[1. -1. 4. 0. 5. ]
```

## 2- Addition and subtraction of arrays

```
>>> z= x+y
>>> print (z)
[5.  2.  9.  7. 11.]
>>> z=x-y
>>>print (z)
[-1.  0. -3.  3. -3.]
```

**\*Important note:** In case of arrays operation of different shapes or sizes, you will see the error message *ValueError: shape mismatch: objects cannot be broadcast to a single shape.*

### Example

```
>>>x= array([1,3,5,6])
>>>y= array([0,1, 2 ])
>>> z= x+y
```

**This will not work**

### 3-Multiplication and division by a constant

It is also possible to multiply or divide an **array** by a **constant**. This multiplies or divides each element in the array by the specified value.

#### Example

```
>>> x= array([2, 1, 3, 5, 4], dtype= float)
```

```
>>> y= array([3, 1, 6, 2, 7], dtype= float)
```

```
>>> z=5*x
```

```
>>>print z
```

```
[10.  5. 15. 25. 20.]
```

```
>>> z= x/2.0
```

```
>>>print z
```

```
[1.  0.5  1.5  2.5  2. ]
```

### 4- Multiplication and division of arrays

Multiplication and division between **arrays** is possible only if they have same lengths

#### Example

```
>>> z= x*y
```

```
>>>print z
```

```
[6.  1. 18. 10. 28]
```

## Example

```
>>>z=x/y
```

```
>>>print z
```

```
[0.6666667 1. 0.5 2.5 0.57142857]
```

## 5- Power and roots

When we intend to raise an array **x** to the **power n**. Every element in the array is raised to the **same** specified **power**.

## Example

Let

```
>>>i= array([2,3,4])
```

```
>>>j= i**2
```

```
>>>print j
```

```
array([4,9,16])
```

```
>>>sqrt(i)
```

```
array([1.414, 1.732 2.])
```

## Vector algebra

Some of the operations that we introduced in the previous sections are also applicable to **vectors** (such as **addition** and **subtraction**).

```
>>> a = array([1, 3, 5], dtype=float)
```

```
>>> b = array([4, 2, 6], dtype=float)
```

We can introduce 3D vector for each as

$$\mathbf{a} = \mathbf{i} + 3\mathbf{j} + 5\mathbf{k}$$

$$\mathbf{b} = 4\mathbf{i} + 2\mathbf{j} + 6\mathbf{k}$$

**Addition** and **subtraction** of vectors can be done :

$$\mathbf{c} = \mathbf{a} + \mathbf{b}$$

$$\mathbf{c} = \mathbf{a} - \mathbf{b}$$

Also we can change or re-scale a vector if we multiply it by a constant such as:

$$\mathbf{c} = 5.3 * \mathbf{a}$$



## Dot and cross product of vectors

There are functions in **NumPy** ready to find out the **dot** and **cross** products between **vectors**. If **a** and **b** are two **vectors**, then the **dot** and **cross** products denoted in python as **dot(a,b)** and **cross (a,b)**.

Example

```
>>>dot (a,b)
```

```
40.0
```

```
>>> cross(a,b)
```

```
array([8., 14., -10.]
```

Also the value (**magnitude**) of a vector can be obtained (which is the **square root** of the **sum** of the **squares** of each **element**) by:

```
>>>linalg.norm(a)
```

```
5.916
```