

EXERCISES

- 1.1 List the elements that are used in an instrumentation system.
- 1.2 Give an example of an electronic instrumentation system employed in engineering analysis.
- 1.3 Give an example of an electronic instrumentation system employed in process monitoring.
- 1.4 Give an example of an electronic instrumentation system employed in process control.
- 1.5 Why is it frequently necessary to conduct an experimental program in conjunction with an analytical engineering analysis?
- 1.6 Why is a combined analytical/experimental approach preferred for an engineering analysis?

- 1.7 Explain the difference between open-loop and closed-loop control.
- 1.8 List several sources of error that must be considered in the design of an instrumentation system.
- 1.9 A recorder is specified accurate to ± 2 percent of full scale and full scale is set at 50 mV. Determine the deviation that can be anticipated. Compute the probable percent error when the instrument is used at $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$, and $\frac{5}{8}$ scale. State the conclusion that can be drawn from the results of your computation.
- 1.10 An instrumentation system that is composed of a transducer, power supply, signal conditioner, amplifier, and recorder will exhibit what accumulated error $\%$ if the accuracies of the individual elements are:

	Case 1	Case 2	Case 3	Case 4
Transducer	0.01	0.01	0.02	0.05
Power supply	0.01	0.01	0.02	0.01
Signal conditioner	0.02	0.01	0.05	0.01
Amplifier	0.02	0.01	0.02	0.01
Recorder	0.03	0.01	0.02	0.01

- 1.11 Define range and span of an instrument.

- 1.12 Determine the error produced by a zero offset Z_o if it is not taken into account in determining the output quantity Q_o .
- 1.13 Determine the error produced if an instrument sensitivity is S_1 instead of the anticipated sensitivity S .
- 1.14 Determine the error produced if an instrument sensitivity is S_1 instead of the anticipated sensitivity S and if a zero offset Z_o is not taken into account in determining the output quantity Q_o .
- 1.15 Give an example of a transducer that produces error because of its influence on the quantity being measured.
- 1.16 Give an example of an instrument with dual sensitivity and explain how it may produce unanticipated error in a measurement.
- 1.17 An amplifier in an instrumentation system exhibits a zero drift of 1 percent of full scale per hour. Determine the error if the measurement of Q_o is taken 2.4 hours after the initial zero was established and if the amplifier is operated at one-half of full scale.
- 1.18 A pressure transducer exhibits a temperature sensitivity of 0.1 units per degree Celsius and a pressure sensitivity of 2.5 units per megapascal. If the temperature changes 20°C during a measurement of a pressure of 120 MPa, determine the error due to the dual sensitivity of the transducer.

- 1.19 The sensitivity of an electrical resistance strain gage is defined as

$$S = \frac{\Delta R/R}{\epsilon}$$

Where ΔR is the resistance change of the gage due to an applied strain ϵ .

R is the resistance of the gage.

If the sensitivity $S = 2.0$ for a gage with a resistance of $120\ \Omega$, compute the sensitivity if the gage is connected to the instrument system with lead wires having a total resistance of $12\ \Omega$.

- 1.20** Determine the apparent strain indicated by the strain gage lead-wire system described in Exercise 1.19 if the lead wires are subjected to a temperature change of 16°C after the initial zero is established for the system. Note that the lead wires change resistance with temperature according to:

$$\Delta R = R \gamma \Delta T$$

where γ is the temperature coefficient of resistance (0.0039/°C for copper).

- 1.21** Describe a suitable transducer for measuring pressure in a shock tube.
- 1.22** Place a weight limit on a transducer used to determine the natural frequency of a clamped circular plate fabricated from aluminum and having a diameter of 250 mm and a thickness of 1 mm.
- 1.23** Describe calibration procedures for:
- (a) A power supply
 - (b) A pressure transducer
 - (c) A Wheatstone bridge
 - (d) An amplifier
 - (e) A voltmeter
- 1.24** Describe a calibration procedure to check the entire instrumentation system if the quantity being measured is:
- (a) Strain
 - (b) Pressure
 - (c) Temperature
 - (d) Displacement
 - (e) Acceleration

Questions on Sensors and Transducers

- 3.1** Briefly describe the difference between a transducer and a sensor.
- 3.2** A slide-wire potentiometer having a length of 200 mm is fabricated by winding wire having a diameter of 0.25 mm around a cylindrical insulating core. Determine the resolution limit of this potentiometer.
- 3.3** If the potentiometer of Exercise 3.2 has a resistance of 1000 Ω and can dissipate 4 W of power, determine the voltage required to maximize the sensitivity. What voltage change corresponds to the resolution limit?
- 3.4** A 10-turn potentiometer with a calibrated dial (100 divisions/turn) is used as a balance resistor in a Wheatstone bridge. If the potentiometer has a resistance of 10 k Ω and a resolution of 0.1 percent, what is the minimum incremental change in resistance ΔR that can be read from the calibrated dial?
- 3.5** Why are potentiometers limited to static or quasi-static applications?

- 3.6 List several advantages of the conductive-film type of potentiometer.
- 3.7 A new elevator must be tested to determine its performance characteristics. Design a displacement transducer that utilizes a 20-turn potentiometer to monitor the position of the elevator over its 50-m range of travel.
- 3.8 Compare the potentiometer and LVDT as displacement sensors with regard to the following characteristics: range, accuracy, resolution, frequency response, reliability, complexity, cost.
- 3.9 List the basic elements of the electronic circuit associated with an LVDT.
- 3.10 Prepare a sketch of the output signal as a function of time for an LVDT with its core located in a fixed off-center position if:
 - (a) The demodulator is functioning
 - (b) The demodulator is removed from the circuit

Signal conditioning circuits

- 4.1 A strain gage with $R_g = 350 \, \Omega$ and $S_g = 2.00$ is used to monitor a sinusoidal signal with an amplitude of $1500 \, \mu\text{in./in.}$ and a frequency of 200 Hz. Determine the output voltage E_o if a constant-voltage potentiometer circuit is used to convert the resistance change to voltage. Assume $E_i = 22 \, \text{V}$ and $r = 5$.
- 4.2 Determine the magnitude of the nonlinear term η for the data of Exercise 4.1.
- 4.3 If the strain gage described in Exercise 4.1 can dissipate 0.5 W, determine the input voltage E_i required to maximize the output voltage E_o .
- 4.4 Determine the circuit sensitivity S_{ci} for the constant-voltage potentiometer circuit described in Exercise 4.1.
- 4.5 Determine the load error \mathcal{L} if the output voltage E_o of Exercise 4.1 is monitored with:
 - (a) An oscilloscope having an input impedance of $10^6 \, \Omega$
 - (b) An oscillograph having an input impedance of $350 \, \Omega$
- 4.6 If a constant-current potentiometer circuit was used in Exercise 4.1 in place of the constant-voltage potentiometer circuit, determine the output voltage E_o if $I = 5 \, \text{mA}$.

- 4.7 Determine the magnitude of the nonlinear term η for the data of Exercise 4.6.
- 4.8 If the strain gage described in Exercise 4.1 can dissipate 0.5 W, determine the current I that should be used with a constant-current potentiometer circuit to maximize the output voltage E_o .
- 4.9 Determine the circuit sensitivity S_{cc} for the constant-current potentiometer circuit of Exercise 4.6.
- 4.10 Determine the circuit sensitivity S_{cc} for the constant-current potentiometer circuit of Exercise 4.8.
- 4.11 Determine the load error \mathcal{L} if the output voltage E_o of Exercise 4.6 is monitored with:
 - (a) An oscilloscope having an input impedance of $10^6 \Omega$
 - (b) An oscillograph having an input impedance of 350Ω
- 4.12 A constant-voltage Wheatstone-bridge circuit is employed with a displacement transducer (potentiometer type) to convert resistance change to output voltage. If the displacement transducer has a total resistance of 1000Ω , then $\Delta R = \pm 500 \Omega$ if the wiper is moved from the center position to either end. If the transducer is placed in arm R_1 of the bridge and, if $R_1 = R_2 = R_3 = R_4 = 500 \Omega$:
 - (a) Determine the magnitude of the nonlinear term η as a function of ΔR .
 - (b) Prepare a graph of η versus ΔR as ΔR varies from -500Ω to $+500 \Omega$.
- 4.13 Determine the output voltage E_o as a function of ΔR for the displacement transducer and Wheatstone bridge described in Exercise 4.12 if $E_i = 12 \text{ V}$.
- 4.14 The nonlinear output voltage of Exercise 4.13 makes data interpretation difficult. How can the Wheatstone-bridge circuit be modified to improve the linearity of the output voltage E_o ?
- 4.15 A strain gage with $R_g = 120 \Omega$, $P_T = 0.2 \text{ W}$, and $S_g = 2.00$ is used in arm R_1 of a constant-voltage Wheatstone bridge. Determine:
 - (a) Values of R_2 , R_3 , and R_4 needed to maximize E_o if the available power supply is limited to 36 V
 - (b) The circuit sensitivity of the bridge of Part (a)
- 4.16 If the strain gage of Exercise 4.15 is subjected to a strain of $900 \mu\text{in./in.}$, determine the output voltage E_o .
- 4.17 Four strain gages are installed on a cantilever beam as shown in Fig. E4.17 to produce a displacement transducer.

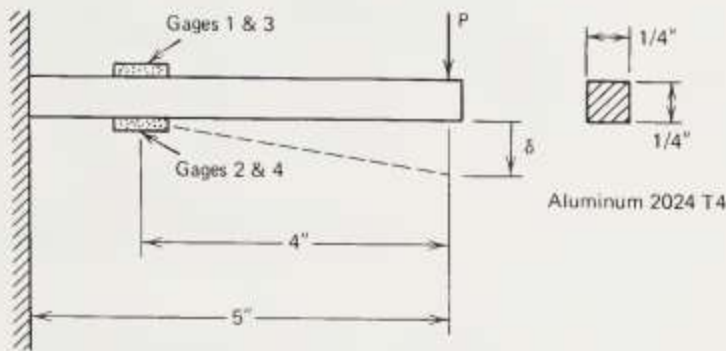


Figure E4.17

- (a) Indicate how the gages should be wired into a Wheatstone bridge to produce maximum signal output.
 - (b) Determine the circuit sensitivity if $R_g = 350 \, \Omega$, $P_T = 0.10 \, \text{W}$, and $S_g = 2.00$.
 - (c) Determine the calibration constant $c = \delta/E_o$ for the transducer.
- 4.18** If the cantilever beam of Exercise 4.17 is used as a load transducer, determine the calibration constant $C = P/E_o$.
- 4.19** A strain gage with $R_g = 120 \, \Omega$, $P_T = 0.2 \, \text{W}$, and $S_g = 2.00$ is used in arm R_1 of a constant-current Wheatstone bridge. Determine:
- (a) Values of R_2 , R_3 , and R_4 needed to maximize E_o if the available power supply can deliver a maximum of 20 mA.
 - (b) The circuit sensitivity of the bridge of Part (a)
 - (c) The output voltage E_o if the gage is subjected to a strain of 900 $\mu\text{in./in.}$
- 4.20** If the displacement transducer of Exercise 4.12 is used with a constant-current Wheatstone bridge:
- (a) Determine the magnitude of the nonlinear term η as a function of ΔR .
 - (b) Prepare a graph of η versus ΔR as ΔR varies from $-500 \, \Omega$ to $+500 \, \Omega$.
- 4.21** Determine the output voltage E_o as a function of ΔR for the displacement transducer and Wheatstone bridge described in Exercise 4.20 if $I = 20 \, \text{mA}$.
- 4.22** Use an op-amp with a gain of 100 dB and $R_a = 7 \, \text{M}\Omega$ to design an inverting amplifier with a gain of 20.
- 4.23** Use an op-amp with a gain of 100 dB and $R_a = 7 \, \text{M}\Omega$ to design a noninverting amplifier with a gain of 20.

Resistance type strain gages

- 5.1 A strain gage is to be fabricated from Advance wire having a diameter of 0.001 in. and a resistance of 25 Ω /in. The gage is to have a gage length of $\frac{1}{4}$ in. and a resistance of 200 Ω . Design a grid configuration.
- 5.2 Plot a family of curves showing bridge voltage E_i as a function of r for a Wheatstone bridge with a single active 350- Ω gage on a material with $P_D = 0.002$ W/mm². Use the area of the gage as a parameter and vary A in increments between 0.0005 mm² to 0.5 mm². From these results, indicate the value of r that should be used in the design of the bridge.
- 5.3 Repeat Exercise 5.2 for a 120- Ω gage.
- 5.4 Determine the system sensitivity for a bridge with a single active gage having $R_g = 350$ Ω and $S_g = 2.05$, if $r = 4$ and if the bridge voltage is 6 V.
- 5.5 If the gage in Exercise 5.4 can dissipate 0.05 W, is the bridge voltage correct? If not, what is the correct voltage?
- 5.6 Determine the voltage output from a Wheatstone bridge if a single active gage is used in an initially balanced bridge to measure a strain of 600 $\mu\text{m/m}$. Assume that a digital voltmeter will be used to measure the voltage and that $S_g = 2.06$, $r = 1$, and $E_i = 9$ V.
- 5.7 Determine the loading error produced by connecting an oscilloscope with an input impedance of 10^6 Ω to a Wheatstone bridge with one active gage. Use $R_g = 350$ Ω , $r = 5$, and $q = 1$.
- 5.8 The bridge in Exercise 5.7 is powered with a 9-V constant-voltage supply and the strain gage has a gage factor $S_g = 3.35$. If the gage responds to a dynamic strain pulse having a magnitude of 1200 $\mu\text{m/m}$, determine the sensitivity setting on the oscilloscope that will give a trace deflection of four divisions.
- 5.9 If the bridge and gage of Exercise 5.8 respond to a strain of 1000 $\mu\text{m/m}$, determine the trace deflection if an oscilloscope having a sensitivity of 1 mV/div is used for the measurement.
- 5.10 If the bridge, gage, and oscilloscope of Exercise 5.9 record a trace deflection of 3.7 divisions, determine the strain at the gage location.
- 5.11 Determine the sensitivity of a gage-bridge-galvanometer system if a four-equal-arm bridge ($R_1 = R_2 = R_3 = R_4 = R_g$) is used and if $R_g = 350$ Ω , $S_g = 2.07$, $P_g = 0.1$ W, $R_G = 100$ Ω , and $S_G = 0.003$ mm/ μA .
- 5.12 Would the sensitivity of the system described in Exercise 5.11 be improved by replacing the 350- Ω gage with a 120- Ω gage? Explain.

Force, Torque and Pressure Measurements

- 6.1 Determine the sensitivity of a load cell–Wheatstone bridge combination if $S_g = 2$, $\nu = 0.30$, $E_i = 6$ V, $A = 0.5$ in.², and $E = 30,000,000$ psi.
- 6.2 The sensitivity of the transducer of Exercise 6.1 can be increased if the input voltage E_i is increased. If each gage in the bridge can dissipate 0.5 W of power, determine the maximum sensitivity that can be achieved without endangering the strain-gage ($R_g = 350$ Ω) sensors.
- 6.3 Determine the voltage ratio E_o/E_i for the load cell of Exercise 6.1 if the fatigue strength of the elastic member is 75,000 psi.
- 6.4 If the load cell of Exercise 6.3 is used in a static load application, what maximum load could be placed on the transducer? What voltage ratio E_o/E_i would result?

- 6.5 The calibration constant of a transducer procured from a commercial supplier is listed as 2 mV/V. Determine the sensitivity S of the transducer if $P_{\max} = 40,000$ lb and $E_i = 10$ V.
- 6.6 Design a beam-type load cell with variable range and sensitivity. Use aluminum ($E = 10,000,000$ psi, $\nu = 0.33$, and $S_f = 20,000$ psi) as the beam material and four electrical resistance strain gages ($S_g = 2$ and $R_g = 120$ Ω) as the sensors. Design the load cell to give the following sensitivities and corresponding range:

$(E_o/E_i)^*$ (mV/V)	Range (lb)
1	1000
2	500
5	200

- 6.7 Design a ring-type load cell with a linear-variable-differential-transformer (LVDT) sensor. The load cell should have a capacity of 2000 lb. The radius to thickness ratio of the ring R/t should be 10. Select an LVDT for this application from Table 3.1. Use steel ($E = 30,000,000$ psi and $\nu = 0.30$) for the ring. Determine the sensitivity S_i for your transducer.
- 6.8 For the transducer designed in Exercise 6.7, determine $(E_o/E_i)^*$ if the fatigue strength of the steel $S_f = 60,000$ psi.
- 6.9 Show that the torque cell shown in Fig. 6.6 is insensitive to both axial load P and moments M_x and M_y .
- 6.10 Determine the sensitivity of a torque cell if $E = 30,000,000$ psi, $\nu = 0.30$, $E_i = 8$ V, $D = 1$ in., $S_g = 2$, and $R_g = 120$ Ω .
- 6.11 The sensitivity of the torque cell described in Exercise 6.10 can be increased if the input voltage E_i is increased. If each gage in the bridge can dissipate 0.8 W of power, determine the maximum sensitivity that can be achieved without endangering the strain-gage sensors.

- 6.12** Determine the sensitivity of the torque cell of Exercise 6.11 if strain gages having $R_g = 500\ \Omega$ are used in place of the $120\text{-}\Omega$ gages.
- 6.13** A torque cell with a capacity of $500\text{ ft} \cdot \text{lbs}$ is supplied with a calibration constant of $(E_o/E_i)^* = 4\text{ mV/V}$ and a recommendation that the input voltage $E_i = 10\text{ V}$. If the cell is used with $E_i = 8\text{ V}$ and a measurement of E_o yields 24 mV , determine the torque T .
- 6.14** Determine the sensitivity of the torque cell described in Exercise 6.13.
- 6.15** Why are at least four slip rings used to transmit the voltages associated with a torque cell on a rotating shaft?
- 6.16** Outline the advantages associated with the use of telemetry for data transmission from a rotating shaft.
- 6.17** A solid circular shaft having a diameter of 2 in. is rotating at 800 rpm and is transmitting 100 hp . Show how four strain gages can be used to

convert the shaft itself into a torque cell. Determine the sensitivity of this shaft-torque transducer if the shaft is made of steel having $E = 30,000,000\text{ psi}$ and $\nu = 0.30$.